The Parma Polyhedra Library
C Language Interface
User's Manual*
(version 0.11.2)

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1 Main Page

All the declarations needed for using the PPL's C interface (preprocessor symbols, data types, variables and functions) are collected in the header file `ppl_c.h`. This file, which is designed to work with pre-ANSI and ANSI C compilers as well as C99 and C++ compilers, should be included, either directly or via some other header file, with the directive

```
#include <ppl_c.h>
```

If this directive does not work, then your compiler is unable to find the file `ppl_c.h`. So check that the library is installed (if it is not installed, you may want to `make install`, perhaps with root privileges) in the right place (if not you may want to reconfigure the library using the appropriate pathname for the `--prefix` option); and that your compiler knows where it is installed (if not you should add the path to the directory where `ppl_c.h` is located to the compiler's include file search path; this is usually done with the `-I` option).

The name space of the PPL's C interface is `PPL_*` for preprocessor symbols, enumeration values and variables; and `ppl_*` for data types and function names. The interface systematically uses *opaque data types* (generic pointers that completely hide the internal representations from the client code) and provides all required access functions. By using just the interface, the client code can exploit all the functionalities of the library yet avoid directly manipulating the library's data structures. The advantages are that (1)

applications do not depend on the internals of the library (these may change from release to release), and (2) the interface invariants can be thoroughly checked (by the access functions).

Note

> All functions taking as input argument an opaque pointer datatype assume that such an argument is actually *referring to a valid PPL object*. For instance, a function with an argument having type `ppl_MIP_Problem_t` will expect a valid MIP_Problem object, previously initialized by calling, e.g., `ppl_new_MIP_Problem`. If that is not the case (e.g., if a null pointer is passed in), the behavior is undefined.

The PPL's C interface is initialized by means of the `ppl_initialize` function. This function must be called *before using any other interface of the library*. The application can release the resources allocated by the library by calling the `ppl_finalize` function. After this function is called *no other interface of the library may be used* until the interface is re-initialized using `ppl_initialize`.

Any application using the PPL should make sure that only the intended version(s) of the library are ever used. The version used can be checked at compile-time thanks to the macros PPL_VERSION_MAJOR, PPL_VERSION_MINOR, PPL_VERSION_REVISION and PPL_VERSION_BETA, which give, respectively major, minor, revision and beta numbers of the PPL version. This is an example of their use:

```
#if PPL_VERSION_MAJOR == 0 && PPL_VERSION_MINOR < 6
# error "PPL version 0.6 or following is required"
#endif
```

Compile-time checking, however, is not normally enough, particularly in an environment where there is dynamic linking. Run-time checking can be performed by means of the functions `ppl_version_major`, `ppl_version_minor`, `ppl_version_revision`, and `ppl_version_beta`. The PPL's C interface also provides functions `ppl_version`, returning character string containing the full version number, and `ppl_banner`, returning a string that, in addition, provides (pointers to) other useful information for the library user.

All programs using the PPL's C interface must link with the following libraries: `libppl_c` (PPL's C interface), `libppl` (PPL's core), `libgmpxx` (GMP's C++ interface), and `libgmp` (GMP's library core). On most Unix-like systems, this is done by adding `-lppl_c`, `-lppl`, `-lgmpxx`, and `-lgmp` to the compiler's or linker's command line. For example:

```
gcc myprogram.o -lppl_c -lppl -lgmpxx -lgmp
```

If this does not work, it means that your compiler/linker is not finding the libraries where it expects. Again, this could be because you forgot to install the library or you installed it in a non-standard location. In the latter case you will need to use the appropriate options (usually `-L`) and, if you use shared libraries, some sort of run-time path selection mechanisms. Consult your compiler's documentation for details. Notice that the PPL is built using `Libtool` and an application can exploit this fact to significantly simplify the linking phase. See Libtool's documentation for details. Those working under Linux can find a lot of useful information on how to use program libraries (including static, shared, and dynamically loaded libraries) in the `Program Library HOWTO`.

For examples on how to use the functions provided by the C interface, you are referred to the directory `demos/ppl_lpsol/` in the source distribution. It contains a *Mixed Integer (Linear) Programming* solver written in C. In order to use this solver you will need to install `GLPK` (the GNU Linear Programming Kit): this is used to read linear programs in MPS format.

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6 Module Documentation

6.1 C Language Interface

The Parma Polyhedra Library comes equipped with an interface for the C language.

6.2 Library Initialization and Finalization

Functions

- int ppl_initialize (void)

  Initializes the Parma Polyhedra Library. This function must be called before any other function.

- int ppl_finalize (void)

  Finalizes the Parma Polyhedra Library. This function must be called after any other function.

- int ppl_set_rounding_for_PPL (void)

  Sets the FPU rounding mode so that the PPL abstractions based on floating point numbers work correctly.

- int ppl_restore_pre_PPL_rounding (void)

  Sets the FPU rounding mode as it was before initialization of the PPL.

- int ppl_irrational_precision (unsigned *p)

  Writes to `p` *the precision parameter used for irrational calculations.*

- int ppl_set_irrational_precision (unsigned p)

  Sets the precision parameter used for irrational calculations.

6.2.1 Detailed Description

Functions for initialization/finalization of the library, as well as setting/resetting of floating-point rounding mode.

6.2.2 Function Documentation

6.2.2.1 int ppl_initialize (void)

Initializes the Parma Polyhedra Library. This function must be called before any other function.

Returns

`PPL_ERROR_INVALID_ARGUMENT` if the library was already initialized.

6.2.2.2 int ppl_finalize (void)

Finalizes the Parma Polyhedra Library. This function must be called after any other function.

Returns

`PPL_ERROR_INVALID_ARGUMENT` if the library was already finalized.

6.2.2.3 int ppl_set_rounding_for_PPL (void)

Sets the FPU rounding mode so that the PPL abstractions based on floating point numbers work correctly.

This is performed automatically at initialization-time. Calling this function is needed only if restore_pre_-PPL_rounding() has been previously called.

6.2.2.4 int ppl_restore_pre_PPL_rounding (void)

Sets the FPU rounding mode as it was before initialization of the PPL.

After calling this function it is absolutely necessary to call set_rounding_for_PPL() before using any PPL abstractions based on floating point numbers. This is performed automatically at finalization-time.

6.2.2.5 int ppl_set_irrational_precision (unsigned *p*)

Sets the precision parameter used for irrational calculations.

If `p` is less than or equal to `INT_MAX`, sets the precision parameter used for irrational calculations to `p`. Then, in the irrational calculations returning an unbounded rational, (e.g., when computing a square root), the lesser between numerator and denominator will be limited to `2**p`.

6.3 Version Checking

Defines

- #define PPL_VERSION "0.11.2"

  A string containing the PPL version.

- #define PPL_VERSION_MAJOR 0

  The major number of the PPL version.

- #define PPL_VERSION_MINOR 11

The minor number of the PPL version.

- #define PPL_VERSION_REVISION 2

  The revision number of the PPL version.

- #define PPL_VERSION_BETA 0

  The beta number of the PPL version. This is zero for official releases and nonzero for development snapshots.

Functions

- int ppl_version_major (void)

  Returns the major number of the PPL version.

- int ppl_version_minor (void)

  Returns the minor number of the PPL version.

- int ppl_version_revision (void)

  Returns the revision number of the PPL version.

- int ppl_version_beta (void)

  Returns the beta number of the PPL version.

- int ppl_version (const char **p)

  Writes to `*p` a pointer to a character string containing the PPL version.

- int ppl_banner (const char **p)

  Writes to `*p` a pointer to a character string containing the PPL banner.

6.3.1 Detailed Description

Symbolic constants and functions related to library version checking.

6.3.2 Define Documentation

6.3.2.1 #define PPL_VERSION "0.11.2"

A string containing the PPL version.

Let `M` and `m` denote the numbers associated to PPL_VERSION_MAJOR and PPL_VERSION_MINOR, respectively. The format of PPL_VERSION is `M "." m` if both PPL_VERSION_REVISION (`r`) and PPL_VERSION_BETA (`b`)are zero, `M "." m "pre" b` if PPL_VERSION_REVISION is zero and PPL_VERSION_BETA is not zero, `M "." m "." r` if PPL_VERSION_REVISION is not zero and PPL_VERSION_BETA is zero, `M "." m "." r "pre" b` if neither PPL_VERSION_REVISION nor PPL_VERSION_BETA are zero.

6.3.3 Function Documentation

6.3.3.1 int ppl_banner (const char ** *p*)

Writes to *p a pointer to a character string containing the PPL banner.

The banner provides information about the PPL version, the licensing, the lack of any warranty whatsoever, the C++ compiler used to build the library, where to report bugs and where to look for further information.

6.4 Error Handling

Enumerations

- enum ppl_enum_error_code {

  PPL_ERROR_OUT_OF_MEMORY, PPL_ERROR_INVALID_ARGUMENT, PPL_ERROR_-DOMAIN_ERROR, PPL_ERROR_LENGTH_ERROR,

  PPL_ARITHMETIC_OVERFLOW, PPL_STDIO_ERROR, PPL_ERROR_INTERNAL_ERROR, PPL_ERROR_UNKNOWN_STANDARD_EXCEPTION,

  PPL_ERROR_UNEXPECTED_ERROR, PPL_TIMEOUT_EXCEPTION, PPL_ERROR_LOGIC_-ERROR }

  Defines the error codes that any function may return.

Functions

- int ppl_set_error_handler (void(*h)(enum ppl_enum_error_code code, const char *description))

  Installs the user-defined error handler pointed at by `h`.

6.4.1 Detailed Description

Symbolic constants and functions related to error reporting/handling.

6.4.2 Enumeration Type Documentation

6.4.2.1 enum ppl_enum_error_code

Defines the error codes that any function may return.

Enumerator:

PPL_ERROR_OUT_OF_MEMORY The virtual memory available to the process has been exhausted.

PPL_ERROR_INVALID_ARGUMENT A function has been invoked with an invalid argument.

PPL_ERROR_DOMAIN_ERROR A function has been invoked outside its domain of definition.

PPL_ERROR_LENGTH_ERROR The construction of an object that would exceed its maximum permitted size was attempted.

PPL_ARITHMETIC_OVERFLOW An arithmetic overflow occurred and the computation was consequently interrupted. This can *only* happen in library's incarnations using bounded integers as coefficients.

PPL_STDIO_ERROR An error occurred during a C input/output operation. A more precise indication of what went wrong is available via `errno`.

PPL_ERROR_INTERNAL_ERROR An internal error that was diagnosed by the PPL itself. This indicates a bug in the PPL.

PPL_ERROR_UNKNOWN_STANDARD_EXCEPTION A standard exception has been raised by the C++ run-time environment. This indicates a bug in the PPL.

PPL_ERROR_UNEXPECTED_ERROR A totally unknown, totally unexpected error happened. This indicates a bug in the PPL.

PPL_TIMEOUT_EXCEPTION An exception has been raised by the PPL as a timeout previously set by the user has expired.

PPL_ERROR_LOGIC_ERROR The client program attempted to use the PPL in a way that violates its internal logic. This happens, for instance, when the client attempts to use the timeout facilities on a system that does not support them.

6.4.3 Function Documentation

6.4.3.1 int ppl_set_error_handler (void(∗)(enum ppl_enum_error_code code, const char ∗description) *h*)

Installs the user-defined error handler pointed at by `h`.

The error handler takes an error code and a textual description that gives further information about the actual error. The C string containing the textual description is read-only and its existence is not guaranteed after the handler has returned.

6.5 Handling

Functions

- int ppl_set_timeout (unsigned time)

  Sets the timeout for computations whose completion could require an exponential amount of time.

- int ppl_reset_timeout (void)

  Resets the timeout time so that the computation is not interrupted.

- int ppl_set_deterministic_timeout (unsigned weight)

  Sets a threshold for computations whose completion could require an exponential amount of time.

- int ppl_reset_deterministic_timeout (void)

  Resets the deterministic timeout so that the computation is not interrupted.

6.5.1 Detailed Description

Functions for setting and resetting timeouts.

6.5.2 Function Documentation

6.5.2.1 int ppl_set_timeout (unsigned *time*)

Sets the timeout for computations whose completion could require an exponential amount of time.

Parameters

time The number of hundreths of seconds. It must be strictly greater than zero.

Computations taking exponential time will be interrupted some time after `time` hundreths of seconds have elapsed since the call to the timeout setting function. If the computation is interrupted that way, the interrupted function will return error code `PPL_TIMEOUT_EXCEPTION`. Otherwise, if the computation completes without being interrupted, then the timeout should be reset by calling `ppl_reset_timeout()`.

6.5.2.2 int ppl_set_deterministic_timeout (unsigned *weight*)

Sets a threshold for computations whose completion could require an exponential amount of time.

Parameters

weight The maximum computational weight allowed. It must be strictly greater than zero.

Computations taking exponential time will be interrupted some time after reaching the `weight` complexity threshold. If the computation is interrupted that way, the interrupted function will return error code `PPL_TIMEOUT_EXCEPTION`. Otherwise, if the computation completes without being interrupted, then the deterministic timeout should be reset by calling `ppl_reset_deterministic_timeout()`.

Note

This "timeout" checking functionality is said to be *deterministic* because it is not based on actual elapsed time. Its behavior will only depend on (some of the) computations performed in the PPL library and it will be otherwise independent from the computation environment (CPU, operating system, compiler, etc.).

Warning

The weight mechanism is under alpha testing. In particular, there is still no clear relation between the weight threshold and the actual computational complexity. As a consequence, client applications should be ready to reconsider the tuning of these weight thresholds when upgrading to newer version of the PPL.

6.6 Library Datatypes

Typedefs for the library datatypes and related symbolic constants.

Typedefs

- typedef size_t ppl_dimension_type

  An unsigned integral type for representing space dimensions.

- typedef const char * ppl_io_variable_output_function_type (ppl_dimension_type var)

  The type of output functions used for printing variables.

- typedef struct ppl_Coefficient_tag * ppl_Coefficient_t

  Opaque pointer.

- typedef struct ppl_Coefficient_tag const * ppl_const_Coefficient_t

  Opaque pointer to const object.

- typedef struct ppl_Linear_Expression_tag * ppl_Linear_Expression_t

  Opaque pointer.

- typedef struct ppl_Linear_Expression_tag const * ppl_const_Linear_Expression_t

  Opaque pointer to const object.

- typedef struct ppl_Constraint_tag * ppl_Constraint_t

  Opaque pointer.

- typedef struct ppl_Constraint_tag const * ppl_const_Constraint_t

  Opaque pointer to const object.

- typedef struct ppl_Constraint_System_tag * ppl_Constraint_System_t

  Opaque pointer.

- typedef struct ppl_Constraint_System_tag const * ppl_const_Constraint_System_t

  Opaque pointer to const object.

- typedef struct ppl_Constraint_System_const_iterator_tag * ppl_Constraint_System_const_iterator_t

  Opaque pointer.

- typedef struct ppl_Constraint_System_const_iterator_tag const * ppl_const_Constraint_System_-const_iterator_t

  Opaque pointer to const object.

- typedef struct ppl_Generator_tag * ppl_Generator_t

  Opaque pointer.

- typedef struct ppl_Generator_tag const * ppl_const_Generator_t

  Opaque pointer to const object.

- typedef struct ppl_Generator_System_tag * ppl_Generator_System_t

  Opaque pointer.

- typedef struct ppl_Generator_System_tag const * ppl_const_Generator_System_t

Opaque pointer to const object.

- typedef struct ppl_Generator_System_const_iterator_tag * ppl_Generator_System_const_iterator_t

  Opaque pointer.

- typedef struct ppl_Generator_System_const_iterator_tag const * ppl_const_Generator_System_-const_iterator_t

  Opaque pointer to const object.

- typedef struct ppl_Congruence_tag * ppl_Congruence_t

  Opaque pointer.

- typedef struct ppl_Congruence_tag const * ppl_const_Congruence_t

  Opaque pointer to const object.

- typedef struct ppl_Congruence_System_tag * ppl_Congruence_System_t

  Opaque pointer.

- typedef struct ppl_Congruence_System_tag const * ppl_const_Congruence_System_t

  Opaque pointer to const object.

- typedef struct ppl_Congruence_System_const_iterator_tag * ppl_Congruence_System_const_-iterator_t

  Opaque pointer.

- typedef struct ppl_Congruence_System_const_iterator_tag const * ppl_const_Congruence_-System_const_iterator_t

  Opaque pointer to const object.

- typedef struct ppl_Grid_Generator_tag * ppl_Grid_Generator_t

  Opaque pointer.

- typedef struct ppl_Grid_Generator_tag const * ppl_const_Grid_Generator_t

  Opaque pointer to const object.

- typedef struct ppl_Grid_Generator_System_tag * ppl_Grid_Generator_System_t

  Opaque pointer.

- typedef struct ppl_Grid_Generator_System_tag const * ppl_const_Grid_Generator_System_t

  Opaque pointer to const object.

- typedef struct ppl_Grid_Generator_System_const_iterator_tag * ppl_Grid_Generator_System_-const_iterator_t

  Opaque pointer.

- typedef struct ppl_Grid_Generator_System_const_iterator_tag const * ppl_const_Grid_Generator_-System_const_iterator_t

  Opaque pointer to const object.

- typedef struct ppl_MIP_Problem_tag * ppl_MIP_Problem_t

Opaque pointer.

- typedef struct ppl_MIP_Problem_tag const * ppl_const_MIP_Problem_t

  Opaque pointer to const object.

- typedef struct ppl_PIP_Problem_tag * ppl_PIP_Problem_t

  Opaque pointer.

- typedef struct ppl_PIP_Problem_tag const * ppl_const_PIP_Problem_t

  Opaque pointer to const object.

- typedef struct ppl_PIP_Tree_Node_tag * ppl_PIP_Tree_Node_t

  Opaque pointer.

- typedef struct ppl_PIP_Tree_Node_tag const * ppl_const_PIP_Tree_Node_t

  Opaque pointer to const object.

- typedef struct ppl_PIP_Decision_Node_tag * ppl_PIP_Decision_Node_t

  Opaque pointer.

- typedef struct ppl_PIP_Decision_Node_tag const * ppl_const_PIP_Decision_Node_t

  Opaque pointer to const object.

- typedef struct ppl_PIP_Solution_Node_tag * ppl_PIP_Solution_Node_t

  Opaque pointer.

- typedef struct ppl_PIP_Solution_Node_tag const * ppl_const_PIP_Solution_Node_t

  Opaque pointer to const object.

- typedef struct ppl_Artificial_Parameter_tag * ppl_Artificial_Parameter_t

  Opaque pointer.

- typedef struct ppl_Artificial_Parameter_tag const * ppl_const_Artificial_Parameter_t

  Opaque pointer to const object.

- typedef struct ppl_Artificial_Parameter_Sequence_tag * ppl_Artificial_Parameter_Sequence_t

  Opaque pointer.

- typedef struct ppl_Artificial_Parameter_Sequence_tag const * ppl_const_Artificial_Parameter_-Sequence_t

  Opaque pointer to const object.

- typedef struct ppl_Artificial_Parameter_Sequence_const_iterator_tag * ppl_Artificial_Parameter_-Sequence_const_iterator_t

  Opaque pointer.

- typedef struct ppl_Artificial_Parameter_Sequence_const_iterator_tag const * ppl_const_Artificial_-Parameter_Sequence_const_iterator_t

  Opaque pointer to const object.

- typedef struct ppl_Polyhedron_tag ∗ ppl_Polyhedron_t

  Opaque pointer.

- typedef struct ppl_Polyhedron_tag const ∗ ppl_const_Polyhedron_t

  Opaque pointer to const object.

- typedef struct ppl_Pointset_Powerset_C_Polyhedron_tag ∗ ppl_Pointset_Powerset_C_Polyhedron_t

  Opaque pointer.

- typedef struct ppl_Pointset_Powerset_C_Polyhedron_tag const ∗ ppl_const_Pointset_Powerset_C_-Polyhedron_t

  Opaque pointer to const object.

- typedef struct ppl_Pointset_Powerset_C_Polyhedron_iterator_tag ∗ ppl_Pointset_Powerset_C_-Polyhedron_iterator_t

  Opaque pointer.

- typedef struct ppl_Pointset_Powerset_C_Polyhedron_iterator_tag const ∗ ppl_const_Pointset_-Powerset_C_Polyhedron_iterator_t

  Opaque pointer to const object.

- typedef struct ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag ∗ ppl_Pointset_Powerset_-C_Polyhedron_const_iterator_t

  Opaque pointer.

- typedef struct ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag const ∗ ppl_const_-Pointset_Powerset_C_Polyhedron_const_iterator_t

  Opaque pointer to const object.

Enumerations

- enum ppl_enum_Constraint_Type {

  PPL_CONSTRAINT_TYPE_LESS_THAN, PPL_CONSTRAINT_TYPE_LESS_OR_EQUAL, PPL_CONSTRAINT_TYPE_EQUAL, PPL_CONSTRAINT_TYPE_GREATER_OR_EQUAL,

  PPL_CONSTRAINT_TYPE_GREATER_THAN }

  Describes the relations represented by a constraint.

- enum ppl_enum_Generator_Type { PPL_GENERATOR_TYPE_LINE, PPL_GENERATOR_-TYPE_RAY, PPL_GENERATOR_TYPE_POINT, PPL_GENERATOR_TYPE_CLOSURE_-POINT }

  Describes the different kinds of generators.

- enum ppl_enum_Grid_Generator_Type { PPL_GRID_GENERATOR_TYPE_LINE, PPL_GRID_-GENERATOR_TYPE_PARAMETER, PPL_GRID_GENERATOR_TYPE_POINT }

  Describes the different kinds of grid generators.

- enum ppl_enum_Bounded_Integer_Type_Width {
  PPL_BITS_8, PPL_BITS_16, PPL_BITS_32, PPL_BITS_64,
  PPL_BITS_128 }

  Widths of bounded integer types.

- enum ppl_enum_Bounded_Integer_Type_Representation { PPL_UNSIGNED, PPL_SIGNED_2_-COMPLEMENT }

  Representation of bounded integer types.

- enum ppl_enum_Bounded_Integer_Type_Overflow { PPL_OVERFLOW_WRAPS, PPL_-OVERFLOW_UNDEFINED, PPL_OVERFLOW_IMPOSSIBLE }

  Overflow behavior of bounded integer types.

Functions

- int ppl_max_space_dimension (ppl_dimension_type *m)

  Writes to `m` the maximum space dimension this library can handle.

- int ppl_not_a_dimension (ppl_dimension_type *m)

  Writes to `m` a value that does not designate a valid dimension.

- int ppl_io_print_variable (ppl_dimension_type var)

  Pretty-prints `var` to `stdout`.

- int ppl_io_fprint_variable (FILE *stream, ppl_dimension_type var)

  Pretty-prints `var` to the given output `stream`.

- int ppl_io_asprint_variable (char **strp, ppl_dimension_type var)

  Pretty-prints `var` to a malloc-allocated string, a pointer to which is returned via `strp`.

- int ppl_io_set_variable_output_function (ppl_io_variable_output_function_type *p)

  Sets the output function to be used for printing variables to `p`.

- int ppl_io_get_variable_output_function (ppl_io_variable_output_function_type **pp)

  Writes a pointer to the current variable output function to `pp`.

- char * ppl_io_wrap_string (const char *src, unsigned indent_depth, unsigned preferred_first_line_-length, unsigned preferred_line_length)

  Utility function for the wrapping of lines of text.

Variables

- unsigned int PPL_COMPLEXITY_CLASS_POLYNOMIAL

  Code of the worst-case polynomial complexity class.

- unsigned int PPL_COMPLEXITY_CLASS_SIMPLEX

  Code of the worst-case exponential but typically polynomial complexity class.

- unsigned int PPL_COMPLEXITY_CLASS_ANY

  Code of the universal complexity class.

- unsigned int PPL_POLY_CON_RELATION_IS_DISJOINT

  Individual bit saying that the polyhedron and the set of points satisfying the constraint are disjoint.

- unsigned int PPL_POLY_CON_RELATION_STRICTLY_INTERSECTS

  Individual bit saying that the polyhedron intersects the set of points satisfying the constraint, but it is not included in it.

- unsigned int PPL_POLY_CON_RELATION_IS_INCLUDED

  Individual bit saying that the polyhedron is included in the set of points satisfying the constraint.

- unsigned int PPL_POLY_CON_RELATION_SATURATES

  Individual bit saying that the polyhedron is included in the set of points saturating the constraint.

- unsigned int PPL_POLY_GEN_RELATION_SUBSUMES

  Individual bit saying that adding the generator would not change the polyhedron.

6.6.1 Detailed Description

Typedefs for the library datatypes and related symbolic constants. The datatypes provided by the library should be manipulated by means of the corresponding opaque pointer types and the functions working on them.

Note

To simplify the detection of common programming mistakes, we provide both pointer-to-const and pointer-to-nonconst opaque pointers, with implicit conversions mapping each pointer-to-nonconst to the corresponding pointer-to-const when needed. The user of the C interface is therefore recommended to adopt the pointer-to-const type whenever read-only access is meant.

6.6.2 Typedef Documentation

6.6.2.1 typedef const char∗ ppl_io_variable_output_function_type(ppl_dimension_type var)

The type of output functions used for printing variables.

An output function for variables must write a textual representation for `var` to a character buffer, null-terminate it, and return a pointer to the beginning of the buffer. In case the operation fails, 0 should be returned and perhaps `errno` should be set in a meaningful way. The library does nothing with the buffer, besides printing its contents.

6.6.3 Enumeration Type Documentation

6.6.3.1 enum ppl_enum_Constraint_Type

Describes the relations represented by a constraint.

Enumerator:

PPL_CONSTRAINT_TYPE_LESS_THAN The constraint is of the form $e < 0$.

PPL_CONSTRAINT_TYPE_LESS_OR_EQUAL The constraint is of the form $e \leq 0$.

PPL_CONSTRAINT_TYPE_EQUAL The constraint is of the form $e = 0$.

PPL_CONSTRAINT_TYPE_GREATER_OR_EQUAL The constraint is of the form $e \geq 0$.

PPL_CONSTRAINT_TYPE_GREATER_THAN The constraint is of the form $e > 0$.

6.6.3.2 enum ppl_enum_Generator_Type

Describes the different kinds of generators.

Enumerator:

PPL_GENERATOR_TYPE_LINE The generator is a line.

PPL_GENERATOR_TYPE_RAY The generator is a ray.

PPL_GENERATOR_TYPE_POINT The generator is a point.

PPL_GENERATOR_TYPE_CLOSURE_POINT The generator is a closure point.

6.6.3.3 enum ppl_enum_Grid_Generator_Type

Describes the different kinds of grid generators.

Enumerator:

PPL_GRID_GENERATOR_TYPE_LINE The grid generator is a line.

PPL_GRID_GENERATOR_TYPE_PARAMETER The grid generator is a parameter.

PPL_GRID_GENERATOR_TYPE_POINT The grid generator is a point.

6.6.3.4 enum ppl_enum_Bounded_Integer_Type_Width

Widths of bounded integer types.

Enumerator:

PPL_BITS_8 8 bits.

PPL_BITS_16 16 bits.

PPL_BITS_32 32 bits.

PPL_BITS_64 64 bits.

PPL_BITS_128 128 bits.

6.6.3.5 enum ppl_enum_Bounded_Integer_Type_Representation

Representation of bounded integer types.

Enumerator:

PPL_UNSIGNED Unsigned binary.

PPL_SIGNED_2_COMPLEMENT Signed binary where negative values are represented by the two's complement of the absolute value.

6.6.3.6 enum ppl_enum_Bounded_Integer_Type_Overflow

Overflow behavior of bounded integer types.

Enumerator:

PPL_OVERFLOW_WRAPS On overflow, wrapping takes place. This means that, for a w-bit bounded integer, the computation happens modulo 2^w.

PPL_OVERFLOW_UNDEFINED On overflow, the result is undefined. This simply means that the result of the operation resulting in an overflow can take any value.

Note

Even though something more serious can happen in the system being analyzed ---due to, e.g., C's undefined behavior---, here we are only concerned with the results of arithmetic operations. It is the responsibility of the analyzer to ensure that other manifestations of undefined behavior are conservatively approximated.

PPL_OVERFLOW_IMPOSSIBLE Overflow is impossible. This is for the analysis of languages where overflow is trapped before it affects the state, for which, thus, any indication that an overflow may have affected the state is necessarily due to the imprecision of the analysis.

6.6.4 Function Documentation

6.6.4.1 char∗ ppl_io_wrap_string (const char ∗ *src*, unsigned *indent_depth*, unsigned *preferred_first_line_length*, unsigned *preferred_line_length*)

Utility function for the wrapping of lines of text.

Parameters

src The source string holding the text to wrap.

indent_depth The indentation depth.

preferred_first_line_length The preferred length for the first line of text.

preferred_line_length The preferred length for all the lines but the first one.

Returns

The wrapped string in a malloc-allocated buffer.

7 Class Documentation

7.1 ppl_Artificial_Parameter_Sequence_const_iterator_tag Interface Reference

Types and functions for iterating on PIP artificial parameters.

`#include <ppl_c_header.h>`

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Artificial_Parameter_Sequence_const_iterator (ppl_Artificial_Parameter_Sequence_const_iterator_t *papit)

  Builds a new 'const iterator' and writes a handle to it at address `papit`.

- int ppl_new_Artificial_Parameter_Sequence_const_iterator_from_Artificial_Parameter_Sequence_const_iterator (ppl_Artificial_Parameter_Sequence_const_iterator_t *papit, ppl_const_Artificial_Parameter_Sequence_const_iterator_t apit)

  Builds a const iterator that is a copy of `apit`; writes a handle for the newly created const iterator at address `papit`.

- int ppl_assign_Artificial_Parameter_Sequence_const_iterator_from_Artificial_Parameter_Sequence_const_iterator (ppl_Artificial_Parameter_Sequence_const_iterator_t dst, ppl_const_Artificial_Parameter_Sequence_const_iterator_t src)

  Assigns a copy of the const iterator `src` to `dst`.

- int ppl_delete_Artificial_Parameter_Sequence_const_iterator (ppl_const_Artificial_Parameter_Sequence_const_iterator_t apit)

  Invalidates the handle `apit`: this makes sure the corresponding resources will eventually be released.

Dereferencing, Incrementing and Equality Testing

- int ppl_Artificial_Parameter_Sequence_const_iterator_dereference (ppl_const_Artificial_Parameter_Sequence_const_iterator_t apit, ppl_const_Artificial_Parameter_t *pap)

  Dereference `apit` writing a const handle to the resulting artificial parameter at address `pap`.

- int ppl_Artificial_Parameter_Sequence_const_iterator_increment (ppl_Artificial_Parameter_Sequence_const_iterator_t apit)

  Increment `apit` so that it "points" to the next artificial parameter.

- int ppl_Artificial_Parameter_Sequence_const_iterator_equal_test (ppl_const_Artificial_Parameter_Sequence_const_iterator_t x, ppl_const_Artificial_Parameter_Sequence_const_iterator_t y)

  Returns a positive integer if the iterators corresponding to `x` and `y` are equal; returns 0 if they are different.

7.1.1 Detailed Description

Types and functions for iterating on PIP artificial parameters.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.2 ppl_Artificial_Parameter_tag Interface Reference

Types and functions for PIP artificial parameters.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

- int ppl_Artificial_Parameter_get_Linear_Expression (ppl_const_Artificial_Parameter_t ap, ppl_-Linear_Expression_t le)

  Copies into `le` the linear expression in artificial parameter `ap`.

- int ppl_Artificial_Parameter_coefficient (ppl_const_Artificial_Parameter_t ap, ppl_dimension_type var, ppl_Coefficient_t n)

  Copies into `n` the coefficient of variable `var` in the artificial parameter `ap`.

- int ppl_Artificial_Parameter_get_inhomogeneous_term (ppl_const_Artificial_Parameter_t ap, ppl_-Coefficient_t n)

  Copies into `n` the inhomogeneous term of the artificial parameter `ap`.

- int ppl_Artificial_Parameter_denominator (ppl_const_Artificial_Parameter_t ap, ppl_Coefficient_t n)

  Copies into `n` the denominator in artificial parameter `ap`.

Input/Output Functions

- int ppl_io_print_Artificial_Parameter (ppl_const_Artificial_Parameter_t x)

  Prints `x` to `stdout`.

- int ppl_io_fprint_Artificial_Parameter (FILE *stream, ppl_const_Artificial_Parameter_t x)

  Prints `x` to the given output `stream`.

- int ppl_io_asprint_Artificial_Parameter (char **strp, ppl_const_Artificial_Parameter_t x)

  Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.

- int ppl_Artificial_Parameter_ascii_dump (ppl_const_Artificial_Parameter_t x, FILE *stream)

  Dumps an ascii representation of `x` on `stream`.

- int ppl_Artificial_Parameter_ascii_load (ppl_Artificial_Parameter_t x, FILE *stream)

  Loads an ascii representation of `x` from `stream`.

7.2.1 Detailed Description

Types and functions for PIP artificial parameters. The types and functions for PIP artificial parameters provide an interface towards *Artificial_Parameter*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.3 ppl_Coefficient_tag Interface Reference

Types and functions for coefficients.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Coefficient (ppl_Coefficient_t *pc)

  Creates a new coefficient with value 0 and writes a handle for the newly created coefficient at address `pc`.

- int ppl_new_Coefficient_from_mpz_t (ppl_Coefficient_t *pc, mpz_t z)

  Creates a new coefficient with the value given by the GMP integer `z` *and writes a handle for the newly created coefficient at address* `pc`.

- int ppl_new_Coefficient_from_Coefficient (ppl_Coefficient_t *pc, ppl_const_Coefficient_t c)

  Builds a coefficient that is a copy of `c`*; writes a handle for the newly created coefficient at address* `pc`.

- int ppl_assign_Coefficient_from_mpz_t (ppl_Coefficient_t dst, mpz_t z)

  Assign to `dst` *the value given by the GMP integer* `z`.

- int ppl_assign_Coefficient_from_Coefficient (ppl_Coefficient_t dst, ppl_const_Coefficient_t src)

  Assigns a copy of the coefficient `src` *to* `dst`.

- int ppl_delete_Coefficient (ppl_const_Coefficient_t c)

  Invalidates the handle `c`*: this makes sure the corresponding resources will eventually be released.*

Read-Only Accessor Functions

- int ppl_Coefficient_to_mpz_t (ppl_const_Coefficient_t c, mpz_t z)

  Sets the value of the GMP integer `z` *to the value of* `c`.

- int ppl_Coefficient_OK (ppl_const_Coefficient_t c)

  Returns a positive integer if `c` *is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if* `c` *is broken. Useful for debugging purposes.*

- int ppl_Coefficient_is_bounded (void)

  Returns a positive integer if coefficients are bounded; returns 0 otherwise.

- int ppl_Coefficient_min (mpz_t min)

  Returns a positive integer if coefficients are bounded, in which case `min` *is set to their minimum value; returns 0 otherwise.*

- int ppl_Coefficient_max (mpz_t max)

  Returns a positive integer if coefficients are bounded, in which case `max` *is set to their maximum value; returns 0 otherwise.*

I/O Functions

- int ppl_io_print_Coefficient (ppl_const_Coefficient_t x)

  Prints `x` *to* `stdout`.

- int ppl_io_fprint_Coefficient (FILE *stream, ppl_const_Coefficient_t x)

  Prints `x` *to the given output* `stream`.

- int ppl_io_asprint_Coefficient (char **strp, ppl_const_Coefficient_t x)

  Prints `x` *to a malloc-allocated string, a pointer to which is returned via* `strp`.

7.3.1 Detailed Description

Types and functions for coefficients. The types and functions for coefficients provide an interface towards *Coefficient*. Depending on configuration, the PPL coefficients may be implemented by the unbounded precision integers provided by GMP (default), or by bounded precision integers (with checks for overflows).

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.4 ppl_Congruence_System_const_iterator_tag Interface Reference

Types and functions for iterating on congruence systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Congruence_System_const_iterator (ppl_Congruence_System_const_iterator_t *pcit)

  Builds a new 'const iterator' and writes a handle to it at address `pcit`.

- int ppl_new_Congruence_System_const_iterator_from_Congruence_System_const_iterator (ppl_Congruence_System_const_iterator_t *pcit, ppl_const_Congruence_System_const_iterator_t cit)

  Builds a const iterator that is a copy of `cit`*; writes a handle for the newly created const iterator at address* `pcit`.

- int ppl_assign_Congruence_System_const_iterator_from_Congruence_System_const_iterator (ppl_Congruence_System_const_iterator_t dst, ppl_const_Congruence_System_const_iterator_t src)

  Assigns a copy of the const iterator `src` *to* `dst`.

- int ppl_delete_Congruence_System_const_iterator (ppl_const_Congruence_System_const_-iterator_t cit)

  Invalidates the handle `cit`*: this makes sure the corresponding resources will eventually be released.*

Dereferencing, Incrementing and Equality Testing

- int ppl_Congruence_System_const_iterator_dereference (ppl_const_Congruence_System_-const_iterator_t cit, ppl_const_Congruence_t *pc)

  Dereference `cit` *writing a const handle to the resulting congruence at address* `pc`.

- int ppl_Congruence_System_const_iterator_increment (ppl_Congruence_System_const_-iterator_t cit)

  Increment `cit` *so that it "points" to the next congruence.*

- int ppl_Congruence_System_const_iterator_equal_test (ppl_const_Congruence_System_const_-iterator_t x, ppl_const_Congruence_System_const_iterator_t y)

  Returns a positive integer if the iterators corresponding to `x` *and* `y` *are equal; returns 0 if they are different.*

7.4.1 Detailed Description

Types and functions for iterating on congruence systems. The types and functions for congruence systems iterators provide read-only access to the elements of a congruence system by interfacing *Congruence_-System::const_iterator*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.5 ppl_Congruence_System_tag Interface Reference

Types and functions for congruence systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Congruence_System (ppl_Congruence_System_t *pcs)

  Builds an empty system of congruences and writes a handle to it at address `pcs`.

- int ppl_new_Congruence_System_zero_dim_empty (ppl_Congruence_System_t *pcs)

  Builds a zero-dimensional, unsatisfiable congruence system and writes a handle to it at address `pcs`.

- int ppl_new_Congruence_System_from_Congruence (ppl_Congruence_System_t *pcs, ppl_-const_Congruence_t c)

  Builds the singleton congruence system containing only a copy of congruence `c`*; writes a handle for the newly created system at address* `pcs`.

- int ppl_new_Congruence_System_from_Congruence_System (ppl_Congruence_System_t *pcs, ppl_const_Congruence_System_t cs)

  Builds a congruence system that is a copy of `cs`*; writes a handle for the newly created system at address* `pcs`.

- int ppl_assign_Congruence_System_from_Congruence_System (ppl_Congruence_System_t dst, ppl_const_Congruence_System_t src)

  Assigns a copy of the congruence system `src` *to* `dst`.

- int ppl_delete_Congruence_System (ppl_const_Congruence_System_t cs)

  Invalidates the handle `cs`*: this makes sure the corresponding resources will eventually be released.*

Functions that Do Not Modify the Congruence System

- int ppl_Congruence_System_space_dimension (ppl_const_Congruence_System_t cs, ppl_-dimension_type *m)

  Writes to `m` *the dimension of the vector space enclosing* `cs`.

- int ppl_Congruence_System_empty (ppl_const_Congruence_System_t cs)

  Returns a positive integer if `cs` *contains no (non-trivial) congruence; returns 0 otherwise.*

- int ppl_Congruence_System_begin (ppl_const_Congruence_System_t cs, ppl_Congruence_-System_const_iterator_t cit)

  Assigns to `cit` *a const iterator "pointing" to the beginning of the congruence system* `cs`.

- int ppl_Congruence_System_end (ppl_const_Congruence_System_t cs, ppl_Congruence_-System_const_iterator_t cit)

  Assigns to `cit` *a const iterator "pointing" past the end of the congruence system* `cs`.

- int ppl_Congruence_System_OK (ppl_const_Congruence_System_t cs)

  Returns a positive integer if `cs` *is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if* `cs` *is broken. Useful for debugging purposes.*

Functions that May Modify the Congruence System

- int ppl_Congruence_System_clear (ppl_Congruence_System_t cs)

  Removes all the congruences from the congruence system `cs` *and sets its space dimension to 0.*

- int ppl_Congruence_System_insert_Congruence (ppl_Congruence_System_t cs, ppl_const_-Congruence_t c)

  Inserts a copy of the congruence `c` *into* `cs`*; the space dimension is increased, if necessary.*

Input/Output Functions

- int ppl_io_print_Congruence_System (ppl_const_Congruence_System_t x)
  Prints x to stdout.
- int ppl_io_fprint_Congruence_System (FILE *stream, ppl_const_Congruence_System_t x)
  Prints x to the given output stream.
- int ppl_io_asprint_Congruence_System (char **strp, ppl_const_Congruence_System_t x)
  Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl_Congruence_System_ascii_dump (ppl_const_Congruence_System_t x, FILE *stream)
  Dumps an ascii representation of x on stream.
- int ppl_Congruence_System_ascii_load (ppl_Congruence_System_t x, FILE *stream)
  Loads an ascii representation of x from stream.

7.5.1 Detailed Description

Types and functions for congruence systems. The types and functions for congruence systems provide an interface towards *Congruence_System*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.6 ppl_Congruence_tag Interface Reference

Types and functions for congruences.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Congruence (ppl_Congruence_t *pc, ppl_const_Linear_Expression_t le, ppl_const_Coefficient_t m)
  Creates the new congruence $le = 0 \pmod{m}$ *and writes a handle for it at address* pc*. The space dimension of the new congruence is equal to the space dimension of* le*.*
- int ppl_new_Congruence_zero_dim_false (ppl_Congruence_t *pc)
  Creates the unsatisfiable (zero-dimension space) congruence $0 = 1 \pmod{0}$ *and writes a handle for it at address* pc*.*
- int ppl_new_Congruence_zero_dim_integrality (ppl_Congruence_t *pc)
  Creates the true (zero-dimension space) congruence $0 = 1 \pmod{1}$*, also known as integrality congruence. A handle for the newly created congruence is written at address* pc*.*
- int ppl_new_Congruence_from_Congruence (ppl_Congruence_t *pc, ppl_const_Congruence_t c)

Builds a congruence that is a copy of `c`; writes a handle for the newly created congruence at address `pc`.

- int ppl_assign_Congruence_from_Congruence (ppl_Congruence_t dst, ppl_const_Congruence_t src)
  Assigns a copy of the congruence `src` to `dst`.

- int ppl_delete_Congruence (ppl_const_Congruence_t c)
  Invalidates the handle `c`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Congruence

- int ppl_Congruence_space_dimension (ppl_const_Congruence_t c, ppl_dimension_type *m)
  Writes to `m` the space dimension of `c`.

- int ppl_Congruence_coefficient (ppl_const_Congruence_t c, ppl_dimension_type var, ppl_Coefficient_t n)
  Copies into `n` the coefficient of variable `var` in congruence `c`.

- int ppl_Congruence_inhomogeneous_term (ppl_const_Congruence_t c, ppl_Coefficient_t n)
  Copies into `n` the inhomogeneous term of congruence `c`.

- int ppl_Congruence_modulus (ppl_const_Congruence_t c, ppl_Coefficient_t m)
  Copies into `m` the modulus of congruence `c`.

- int ppl_Congruence_OK (ppl_const_Congruence_t c)
  Returns a positive integer if `c` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `c` is broken. Useful for debugging purposes.

Input/Output Functions

- int ppl_io_print_Congruence (ppl_const_Congruence_t x)
  Prints `x` to `stdout`.

- int ppl_io_fprint_Congruence (FILE *stream, ppl_const_Congruence_t x)
  Prints `x` to the given output `stream`.

- int ppl_io_asprint_Congruence (char **strp, ppl_const_Congruence_t x)
  Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.

- int ppl_Congruence_ascii_dump (ppl_const_Congruence_t x, FILE *stream)
  Dumps an ascii representation of `x` on `stream`.

- int ppl_Congruence_ascii_load (ppl_Congruence_t x, FILE *stream)
  Loads an ascii representation of `x` from `stream`.

7.6.1 Detailed Description

Types and functions for congruences. The types and functions for congruences provide an interface towards *Congruence*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.7 ppl_Constraint_System_const_iterator_tag Interface Reference

Types and functions for iterating on constraint systems.

`#include <ppl_c_header.h>`

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Constraint_System_const_iterator (ppl_Constraint_System_const_iterator_t *pcit)
  Builds a new 'const iterator' and writes a handle to it at address `pcit`.
- int ppl_new_Constraint_System_const_iterator_from_Constraint_System_const_iterator (ppl_Constraint_System_const_iterator_t *pcit, ppl_const_Constraint_System_const_iterator_t cit)
  Builds a const iterator that is a copy of `cit`; writes a handle for the newly created const iterator at address `pcit`.
- int ppl_assign_Constraint_System_const_iterator_from_Constraint_System_const_iterator (ppl_Constraint_System_const_iterator_t dst, ppl_const_Constraint_System_const_iterator_t src)
  Assigns a copy of the const iterator `src` to `dst`.
- int ppl_delete_Constraint_System_const_iterator (ppl_const_Constraint_System_const_iterator_t cit)
  Invalidates the handle `cit`: this makes sure the corresponding resources will eventually be released.

Dereferencing, Incrementing and Equality Testing

- int ppl_Constraint_System_const_iterator_dereference (ppl_const_Constraint_System_const_iterator_t cit, ppl_const_Constraint_t *pc)
  Dereference `cit` writing a const handle to the resulting constraint at address `pc`.
- int ppl_Constraint_System_const_iterator_increment (ppl_Constraint_System_const_iterator_t cit)
  Increment `cit` so that it "points" to the next constraint.
- int ppl_Constraint_System_const_iterator_equal_test (ppl_const_Constraint_System_const_iterator_t x, ppl_const_Constraint_System_const_iterator_t y)
  Returns a positive integer if the iterators corresponding to `x` and `y` are equal; returns 0 if they are different.

7.7.1 Detailed Description

Types and functions for iterating on constraint systems. The types and functions for constraint systems iterators provide read-only access to the elements of a constraint system by interfacing *Constraint_System::const_iterator*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.8 ppl_Constraint_System_tag Interface Reference

Types and functions for constraint systems.

`#include <ppl_c_header.h>`

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Constraint_System (ppl_Constraint_System_t *pcs)
  Builds an empty system of constraints and writes a handle to it at address `pcs`.

- int ppl_new_Constraint_System_zero_dim_empty (ppl_Constraint_System_t *pcs)
  Builds a zero-dimensional, unsatisfiable constraint system and writes a handle to it at address `pcs`.

- int ppl_new_Constraint_System_from_Constraint (ppl_Constraint_System_t *pcs, ppl_const_Constraint_t c)
  Builds the singleton constraint system containing only a copy of constraint `c`; writes a handle for the newly created system at address `pcs`.

- int ppl_new_Constraint_System_from_Constraint_System (ppl_Constraint_System_t *pcs, ppl_const_Constraint_System_t cs)
  Builds a constraint system that is a copy of `cs`; writes a handle for the newly created system at address `pcs`.

- int ppl_assign_Constraint_System_from_Constraint_System (ppl_Constraint_System_t dst, ppl_const_Constraint_System_t src)
  Assigns a copy of the constraint system `src` to `dst`.

- int ppl_delete_Constraint_System (ppl_const_Constraint_System_t cs)
  Invalidates the handle `cs`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Constraint System

- int ppl_Constraint_System_space_dimension (ppl_const_Constraint_System_t cs, ppl_dimension_type *m)
  Writes to `m` the dimension of the vector space enclosing `cs`.

- int ppl_Constraint_System_empty (ppl_const_Constraint_System_t cs)
  Returns a positive integer if `cs` contains no (non-trivial) constraint; returns 0 otherwise.

- int ppl_Constraint_System_has_strict_inequalities (ppl_const_Constraint_System_t cs)
  Returns a positive integer if `cs` contains any (non-trivial) strict inequality; returns 0 otherwise.

- int ppl_Constraint_System_begin (ppl_const_Constraint_System_t cs, ppl_Constraint_System_const_iterator_t cit)
  Assigns to `cit` a const iterator "pointing" to the beginning of the constraint system `cs`.

- int ppl_Constraint_System_end (ppl_const_Constraint_System_t cs, ppl_Constraint_System_const_iterator_t cit)

Assigns to `cit` a const iterator "pointing" past the end of the constraint system `cs`.

- int ppl_Constraint_System_OK (ppl_const_Constraint_System_t cs)

  Returns a positive integer if `cs` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `cs` is broken. Useful for debugging purposes.

Functions that May Modify the Constraint System

- int ppl_Constraint_System_clear (ppl_Constraint_System_t cs)

  Removes all the constraints from the constraint system `cs` and sets its space dimension to 0.

- int ppl_Constraint_System_insert_Constraint (ppl_Constraint_System_t cs, ppl_const_Constraint_t c)

  Inserts a copy of the constraint `c` into `cs`; the space dimension is increased, if necessary.

Input/Output Functions

- int ppl_io_print_Constraint_System (ppl_const_Constraint_System_t x)

  Prints `x` to `stdout`.

- int ppl_io_fprint_Constraint_System (FILE *stream, ppl_const_Constraint_System_t x)

  Prints `x` to the given output `stream`.

- int ppl_io_asprint_Constraint_System (char **strp, ppl_const_Constraint_System_t x)

  Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.

- int ppl_Constraint_System_ascii_dump (ppl_const_Constraint_System_t x, FILE *stream)

  Dumps an ascii representation of `x` on `stream`.

- int ppl_Constraint_System_ascii_load (ppl_Constraint_System_t x, FILE *stream)

  Loads an ascii representation of `x` from `stream`.

7.8.1 Detailed Description

Types and functions for constraint systems. The types and functions for constraint systems provide an interface towards *Constraint_System*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.9 ppl_Constraint_tag Interface Reference

Types and functions for constraints.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Constraint (ppl_Constraint_t *pc, ppl_const_Linear_Expression_t le, enum ppl_-enum_Constraint_Type rel)

  Creates the new constraint '`le rel 0`' and writes a handle for it at address `pc`. The space dimension of the new constraint is equal to the space dimension of `le`.

- int ppl_new_Constraint_zero_dim_false (ppl_Constraint_t *pc)

  Creates the unsatisfiable (zero-dimension space) constraint $0 = 1$ *and writes a handle for it at address `pc`.*

- int ppl_new_Constraint_zero_dim_positivity (ppl_Constraint_t *pc)

  Creates the true (zero-dimension space) constraint $0 \leq 1$*, also known as positivity constraint. A handle for the newly created constraint is written at address `pc`.*

- int ppl_new_Constraint_from_Constraint (ppl_Constraint_t *pc, ppl_const_Constraint_t c)

  Builds a constraint that is a copy of `c`; writes a handle for the newly created constraint at address `pc`.

- int ppl_assign_Constraint_from_Constraint (ppl_Constraint_t dst, ppl_const_Constraint_t src)

  Assigns a copy of the constraint `src` to `dst`.

- int ppl_delete_Constraint (ppl_const_Constraint_t c)

  Invalidates the handle `c`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Constraint

- int ppl_Constraint_space_dimension (ppl_const_Constraint_t c, ppl_dimension_type *m)

  Writes to `m` the space dimension of `c`.

- int ppl_Constraint_type (ppl_const_Constraint_t c)

  Returns the type of constraint `c`.

- int ppl_Constraint_coefficient (ppl_const_Constraint_t c, ppl_dimension_type var, ppl_-Coefficient_t n)

  Copies into `n` the coefficient of variable `var` in constraint `c`.

- int ppl_Constraint_inhomogeneous_term (ppl_const_Constraint_t c, ppl_Coefficient_t n)

  Copies into `n` the inhomogeneous term of constraint `c`.

- int ppl_Constraint_OK (ppl_const_Constraint_t c)

  Returns a positive integer if `c` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `c` is broken. Useful for debugging purposes.

Input/Output Functions

- int ppl_io_print_Constraint (ppl_const_Constraint_t x)

  Prints `x` to `stdout`.

- int ppl_io_fprint_Constraint (FILE *stream, ppl_const_Constraint_t x)
  Prints `x` *to the given output* `stream`.
- int ppl_io_asprint_Constraint (char **strp, ppl_const_Constraint_t x)
  Prints `x` *to a malloc-allocated string, a pointer to which is returned via* `strp`.
- int ppl_Constraint_ascii_dump (ppl_const_Constraint_t x, FILE *stream)
  Dumps an ascii representation of `x` *on* `stream`.
- int ppl_Constraint_ascii_load (ppl_Constraint_t x, FILE *stream)
  Loads an ascii representation of `x` *from* `stream`.

7.9.1 Detailed Description

Types and functions for constraints. The types and functions for constraints provide an interface towards *Constraint*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.10 ppl_Generator_System_const_iterator_tag Interface Reference

Types and functions for iterating on generator systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Generator_System_const_iterator (ppl_Generator_System_const_iterator_t *pgit)
  Builds a new 'const iterator' and writes a handle to it at address `pgit`.
- int ppl_new_Generator_System_const_iterator_from_Generator_System_const_iterator (ppl_-Generator_System_const_iterator_t *pgit, ppl_const_Generator_System_const_iterator_t git)
  Builds a const iterator that is a copy of `git`*; writes a handle for the newly created const iterator at address* `pgit`.
- int ppl_assign_Generator_System_const_iterator_from_Generator_System_const_iterator (ppl_-Generator_System_const_iterator_t dst, ppl_const_Generator_System_const_iterator_t src)
  Assigns a copy of the const iterator `src` *to* `dst`.
- int ppl_delete_Generator_System_const_iterator (ppl_const_Generator_System_const_iterator_t git)
  Invalidates the handle `git`*: this makes sure the corresponding resources will eventually be released.*

Dereferencing, Incrementing and Equality Testing

- int ppl_Generator_System_const_iterator_dereference (ppl_const_Generator_System_const_iterator_t git, ppl_const_Generator_t *pg)

  Dereference `git` writing a const handle to the resulting generator at address `pg`.

- int ppl_Generator_System_const_iterator_increment (ppl_Generator_System_const_iterator_t git)

  Increment `git` so that it "points" to the next generator.

- int ppl_Generator_System_const_iterator_equal_test (ppl_const_Generator_System_const_iterator_t x, ppl_const_Generator_System_const_iterator_t y)

  Returns a positive integer if the iterators corresponding to `x` and `y` are equal; returns 0 if they are different.

7.10.1 Detailed Description

Types and functions for iterating on generator systems. The types and functions for generator systems iterators provide read-only access to the elements of a generator system by interfacing *Generator_System::const_iterator*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.11 ppl_Generator_System_tag Interface Reference

Types and functions for generator systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Generator_System (ppl_Generator_System_t *pgs)

  Builds an empty system of generators and writes a handle to it at address `pgs`.

- int ppl_new_Generator_System_from_Generator (ppl_Generator_System_t *pgs, ppl_const_Generator_t g)

  Builds the singleton generator system containing only a copy of generator `g`; writes a handle for the newly created system at address `pgs`.

- int ppl_new_Generator_System_from_Generator_System (ppl_Generator_System_t *pgs, ppl_const_Generator_System_t gs)

  Builds a generator system that is a copy of `gs`; writes a handle for the newly created system at address `pgs`.

- int ppl_assign_Generator_System_from_Generator_System (ppl_Generator_System_t dst, ppl_const_Generator_System_t src)

  Assigns a copy of the generator system `src` to `dst`.

- int ppl_delete_Generator_System (ppl_const_Generator_System_t gs)
  Invalidates the handle `gs`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Generator System

- int ppl_Generator_System_space_dimension (ppl_const_Generator_System_t gs, ppl_dimension_type *m)
  Writes to `m` the dimension of the vector space enclosing `gs`.
- int ppl_Generator_System_empty (ppl_const_Generator_System_t gs)
  Returns a positive integer if `gs` contains no generators; returns 0 otherwise.
- int ppl_Generator_System_begin (ppl_const_Generator_System_t gs, ppl_Generator_System_const_iterator_t git)
  Assigns to `git` a const iterator "pointing" to the beginning of the generator system `gs`.
- int ppl_Generator_System_end (ppl_const_Generator_System_t gs, ppl_Generator_System_const_iterator_t git)
  Assigns to `git` a const iterator "pointing" past the end of the generator system `gs`.
- int ppl_Generator_System_OK (ppl_const_Generator_System_t gs)
  Returns a positive integer if `gs` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `gs` is broken. Useful for debugging purposes.

Functions that May Modify the Generator System

- int ppl_Generator_System_clear (ppl_Generator_System_t gs)
  Removes all the generators from the generator system `gs` and sets its space dimension to 0.
- int ppl_Generator_System_insert_Generator (ppl_Generator_System_t gs, ppl_const_Generator_t g)
  Inserts a copy of the generator `g` into `gs`; the space dimension is increased, if necessary.

Input/Output Functions

- int ppl_io_print_Generator_System (ppl_const_Generator_System_t x)
  Prints `x` to `stdout`.
- int ppl_io_fprint_Generator_System (FILE *stream, ppl_const_Generator_System_t x)
  Prints `x` to the given output `stream`.
- int ppl_io_asprint_Generator_System (char **strp, ppl_const_Generator_System_t x)
  Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.
- int ppl_Generator_System_ascii_dump (ppl_const_Generator_System_t x, FILE *stream)
  Dumps an ascii representation of `x` on `stream`.
- int ppl_Generator_System_ascii_load (ppl_Generator_System_t x, FILE *stream)
  Loads an ascii representation of `x` from `stream`.

7.11.1 Detailed Description

Types and functions for generator systems. The types and functions for generator systems provide an interface towards *Generator_System*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.12 ppl_Generator_tag Interface Reference

Types and functions for generators.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Generator (ppl_Generator_t *pg, ppl_const_Linear_Expression_t le, enum ppl_enum_Generator_Type t, ppl_const_Coefficient_t d)

  Creates a new generator of direction `le` and type `t`. If the generator to be created is a point or a closure point, the divisor `d` is applied to `le`. For other types of generators `d` is simply disregarded. A handle for the new generator is written at address `pg`. The space dimension of the new generator is equal to the space dimension of `le`.

- int ppl_new_Generator_zero_dim_point (ppl_Generator_t *pg)

  Creates the point that is the origin of the zero-dimensional space $\mathbb{R}^0$. Writes a handle for the new generator at address `pg`.

- int ppl_new_Generator_zero_dim_closure_point (ppl_Generator_t *pg)

  Creates, as a closure point, the point that is the origin of the zero-dimensional space $\mathbb{R}^0$. Writes a handle for the new generator at address `pg`.

- int ppl_new_Generator_from_Generator (ppl_Generator_t *pg, ppl_const_Generator_t g)

  Builds a generator that is a copy of `g`; writes a handle for the newly created generator at address `pg`.

- int ppl_assign_Generator_from_Generator (ppl_Generator_t dst, ppl_const_Generator_t src)

  Assigns a copy of the generator `src` to `dst`.

- int ppl_delete_Generator (ppl_const_Generator_t g)

  Invalidates the handle `g`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Generator

- int ppl_Generator_space_dimension (ppl_const_Generator_t g, ppl_dimension_type *m)

  Writes to `m` the space dimension of `g`.

- int ppl_Generator_type (ppl_const_Generator_t g)

  Returns the type of generator `g`.

- int ppl_Generator_coefficient (ppl_const_Generator_t g, ppl_dimension_type var, ppl_Coefficient_t n)

  Copies into `n` the coefficient of variable `var` in generator `g`.

- int ppl_Generator_divisor (ppl_const_Generator_t g, ppl_Coefficient_t n)

  If `g` is a point or a closure point assigns its divisor to `n`.

- int ppl_Generator_OK (ppl_const_Generator_t g)

  Returns a positive integer if `g` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `g` is broken. Useful for debugging purposes.

Input/Output Functions

- int ppl_io_print_Generator (ppl_const_Generator_t x)

  Prints `x` to `stdout`.

- int ppl_io_fprint_Generator (FILE *stream, ppl_const_Generator_t x)

  Prints `x` to the given output `stream`.

- int ppl_io_asprint_Generator (char **strp, ppl_const_Generator_t x)

  Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.

- int ppl_Generator_ascii_dump (ppl_const_Generator_t x, FILE *stream)

  Dumps an ascii representation of `x` on `stream`.

- int ppl_Generator_ascii_load (ppl_Generator_t x, FILE *stream)

  Loads an ascii representation of `x` from `stream`.

7.12.1 Detailed Description

Types and functions for generators. The types and functions for generators provide an interface towards *Generator*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.13 ppl_Grid_Generator_System_const_iterator_tag Interface Reference

Types and functions for iterating on grid generator systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Grid_Generator_System_const_iterator (ppl_Grid_Generator_System_const_iterator_t *pgit)

  Builds a new 'const iterator' and writes a handle to it at address `pgit`.

- int ppl_new_Grid_Generator_System_const_iterator_from_Grid_Generator_System_const_iterator (ppl_Grid_Generator_System_const_iterator_t *pgit, ppl_const_Grid_Generator_System_const_iterator_t git)

  Builds a const iterator that is a copy of `git`*; writes a handle for the newly created const iterator at address* `pgit`.

- int ppl_assign_Grid_Generator_System_const_iterator_from_Grid_Generator_System_const_iterator (ppl_Grid_Generator_System_const_iterator_t dst, ppl_const_Grid_Generator_System_const_iterator_t src)

  Assigns a copy of the const iterator `src` *to* `dst`.

- int ppl_delete_Grid_Generator_System_const_iterator (ppl_const_Grid_Generator_System_const_iterator_t git)

  Invalidates the handle `git`*: this makes sure the corresponding resources will eventually be released.*

Dereferencing, Incrementing and Equality Testing

- int ppl_Grid_Generator_System_const_iterator_dereference (ppl_const_Grid_Generator_System_const_iterator_t git, ppl_const_Grid_Generator_t *pg)

  Dereference `git` *writing a const handle to the resulting grid generator at address* `pg`.

- int ppl_Grid_Generator_System_const_iterator_increment (ppl_Grid_Generator_System_const_iterator_t git)

  Increment `git` *so that it "points" to the next grid generator.*

- int ppl_Grid_Generator_System_const_iterator_equal_test (ppl_const_Grid_Generator_System_const_iterator_t x, ppl_const_Grid_Generator_System_const_iterator_t y)

  Returns a positive integer if the iterators corresponding to `x` *and* `y` *are equal; returns 0 if they are different.*

7.13.1 Detailed Description

Types and functions for iterating on grid generator systems. The types and functions for grid generator systems iterators provide read-only access to the elements of a grid generator system by interfacing *Grid_Generator_System::const_iterator*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.14 ppl_Grid_Generator_System_tag Interface Reference

Types and functions for grid generator systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Grid_Generator_System (ppl_Grid_Generator_System_t *pgs)

  Builds an empty system of grid generators and writes a handle to it at address `pgs`.

- int ppl_new_Grid_Generator_System_from_Grid_Generator (ppl_Grid_Generator_System_t *pgs, ppl_const_Grid_Generator_t g)

  Builds the singleton grid generator system containing only a copy of generator `g`*; writes a handle for the newly created system at address* `pgs`.

- int ppl_new_Grid_Generator_System_from_Grid_Generator_System (ppl_Grid_Generator_System_t *pgs, ppl_const_Grid_Generator_System_t gs)

  Builds a grid generator system that is a copy of `gs`*; writes a handle for the newly created system at address* `pgs`.

- int ppl_assign_Grid_Generator_System_from_Grid_Generator_System (ppl_Grid_Generator_System_t dst, ppl_const_Grid_Generator_System_t src)

  Assigns a copy of the grid generator system `src` *to* `dst`.

- int ppl_delete_Grid_Generator_System (ppl_const_Grid_Generator_System_t gs)

  Invalidates the handle `gs`*: this makes sure the corresponding resources will eventually be released.*

Functions that Do Not Modify the Grid Generator System

- int ppl_Grid_Generator_System_space_dimension (ppl_const_Grid_Generator_System_t gs, ppl_dimension_type *m)

  Writes to `m` *the dimension of the vector space enclosing* `gs`.

- int ppl_Grid_Generator_System_empty (ppl_const_Grid_Generator_System_t gs)

  Returns a positive integer if `gs` *contains no generator; returns 0 otherwise.*

- int ppl_Grid_Generator_System_begin (ppl_const_Grid_Generator_System_t gs, ppl_Grid_Generator_System_const_iterator_t git)

  Assigns to `git` *a const iterator "pointing" to the beginning of the grid generator system* `gs`.

- int ppl_Grid_Generator_System_end (ppl_const_Grid_Generator_System_t gs, ppl_Grid_Generator_System_const_iterator_t git)

  Assigns to `git` *a const iterator "pointing" past the end of the grid generator system* `gs`.

- int ppl_Grid_Generator_System_OK (ppl_const_Grid_Generator_System_t gs)

  Returns a positive integer if `gs` *is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if* `gs` *is broken. Useful for debugging purposes.*

Functions that May Modify the Grid Generator System

- int ppl_Grid_Generator_System_clear (ppl_Grid_Generator_System_t gs)

  Removes all the generators from the grid generator system `gs` *and sets its space dimension to 0.*

- int ppl_Grid_Generator_System_insert_Grid_Generator (ppl_Grid_Generator_System_t gs, ppl_const_Grid_Generator_t g)

  Inserts a copy of the grid generator `g` into `gs`; the space dimension is increased, if necessary.

Input/Output Functions

- int ppl_io_print_Grid_Generator_System (ppl_const_Grid_Generator_System_t x)

  Prints `x` to `stdout`.

- int ppl_io_fprint_Grid_Generator_System (FILE *stream, ppl_const_Grid_Generator_System_t x)

  Prints `x` to the given output `stream`.

- int ppl_io_asprint_Grid_Generator_System (char **strp, ppl_const_Grid_Generator_System_t x)

  Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.

- int ppl_Grid_Generator_System_ascii_dump (ppl_const_Grid_Generator_System_t x, FILE *stream)

  Dumps an ascii representation of `x` on `stream`.

- int ppl_Grid_Generator_System_ascii_load (ppl_Grid_Generator_System_t x, FILE *stream)

  Loads an ascii representation of `x` from `stream`.

7.14.1 Detailed Description

Types and functions for grid generator systems. The types and functions for grid generator systems provide an interface towards *Grid_Generator_System*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.15 ppl_Grid_Generator_tag Interface Reference

Types and functions for grid generators.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Grid_Generator (ppl_Grid_Generator_t *pg, ppl_const_Linear_Expression_t le, enum ppl_enum_Grid_Generator_Type t, ppl_const_Coefficient_t d)

  Creates a new grid generator of direction `le` and type `t`. If the grid generator to be created is a point or a parameter, the divisor `d` is applied to `le`. If it is a line, `d` is simply disregarded. A handle for the new grid generator is written at address `pg`. The space dimension of the new grid generator is equal to the space dimension of `le`.

- int ppl_new_Grid_Generator_zero_dim_point (ppl_Grid_Generator_t *pg)
  Creates the point that is the origin of the zero-dimensional space $\mathbb{R}^0$. Writes a handle for the new grid generator at address `pg`.

- int ppl_new_Grid_Generator_from_Grid_Generator (ppl_Grid_Generator_t *pg, ppl_const_Grid_Generator_t g)
  Builds a grid generator that is a copy of `g`*; writes a handle for the newly created grid generator at address* `pg`.

- int ppl_assign_Grid_Generator_from_Grid_Generator (ppl_Grid_Generator_t dst, ppl_const_Grid_Generator_t src)
  Assigns a copy of the grid generator `src` *to* `dst`.

- int ppl_delete_Grid_Generator (ppl_const_Grid_Generator_t g)
  Invalidates the handle `g`*: this makes sure the corresponding resources will eventually be released.*

Functions that Do Not Modify the Grid Generator

- int ppl_Grid_Generator_space_dimension (ppl_const_Grid_Generator_t g, ppl_dimension_type *m)
  Writes to `m` *the space dimension of* `g`.

- int ppl_Grid_Generator_type (ppl_const_Grid_Generator_t g)
  Returns the type of grid generator `g`.

- int ppl_Grid_Generator_coefficient (ppl_const_Grid_Generator_t g, ppl_dimension_type var, ppl_Coefficient_t n)
  Copies into `n` *the coefficient of variable* `var` *in grid generator* `g`.

- int ppl_Grid_Generator_divisor (ppl_const_Grid_Generator_t g, ppl_Coefficient_t n)
  If `g` *is a point or a parameter assigns its divisor to* `n`.

- int ppl_Grid_Generator_OK (ppl_const_Grid_Generator_t g)
  Returns a positive integer if `g` *is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if* `g` *is broken. Useful for debugging purposes.*

Input/Output Functions

- int ppl_io_print_Grid_Generator (ppl_const_Grid_Generator_t x)
  Prints `x` *to* `stdout`.

- int ppl_io_fprint_Grid_Generator (FILE *stream, ppl_const_Grid_Generator_t x)
  Prints `x` *to the given output* `stream`.

- int ppl_io_asprint_Grid_Generator (char **strp, ppl_const_Grid_Generator_t x)
  Prints `x` *to a malloc-allocated string, a pointer to which is returned via* `strp`.

- int ppl_Grid_Generator_ascii_dump (ppl_const_Grid_Generator_t x, FILE *stream)
  Dumps an ascii representation of `x` *on* `stream`.

- int ppl_Grid_Generator_ascii_load (ppl_Grid_Generator_t x, FILE *stream)
  Loads an ascii representation of `x` *from* `stream`.

7.15.1 Detailed Description

Types and functions for grid generators. The types and functions for grid generators provide an interface towards *Grid_Generator*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.16 ppl_Linear_Expression_tag Interface Reference

Types and functions for linear expressions.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Linear_Expression (ppl_Linear_Expression_t *ple)

  Creates a new linear expression corresponding to the constant 0 in a zero-dimensional space; writes a handle for the new linear expression at address `ple`.

- int ppl_new_Linear_Expression_with_dimension (ppl_Linear_Expression_t *ple, ppl_dimension_type d)

  Creates a new linear expression corresponding to the constant 0 in a `d`*-dimensional space; writes a handle for the new linear expression at address* `ple`.

- int ppl_new_Linear_Expression_from_Linear_Expression (ppl_Linear_Expression_t *ple, ppl_const_Linear_Expression_t le)

  Builds a linear expression that is a copy of `le`*; writes a handle for the newly created linear expression at address* `ple`.

- int ppl_new_Linear_Expression_from_Constraint (ppl_Linear_Expression_t *ple, ppl_const_Constraint_t c)

  Builds a linear expression corresponding to constraint `c`*; writes a handle for the newly created linear expression at address* `ple`.

- int ppl_new_Linear_Expression_from_Generator (ppl_Linear_Expression_t *ple, ppl_const_Generator_t g)

  Builds a linear expression corresponding to generator `g`*; writes a handle for the newly created linear expression at address* `ple`.

- int ppl_new_Linear_Expression_from_Congruence (ppl_Linear_Expression_t *ple, ppl_const_Congruence_t c)

  Builds a linear expression corresponding to congruence `c`*; writes a handle for the newly created linear expression at address* `ple`.

- int ppl_new_Linear_Expression_from_Grid_Generator (ppl_Linear_Expression_t *ple, ppl_const_Grid_Generator_t g)

  Builds a linear expression corresponding to grid generator `g`*; writes a handle for the newly created linear expression at address* `ple`.

- int ppl_assign_Linear_Expression_from_Linear_Expression (ppl_Linear_Expression_t dst, ppl_-const_Linear_Expression_t src)

  Assigns a copy of the linear expression `src` *to* `dst`.

- int ppl_delete_Linear_Expression (ppl_const_Linear_Expression_t le)

  Invalidates the handle `le`*: this makes sure the corresponding resources will eventually be released.*

Functions that Do Not Modify the Linear Expression

- int ppl_Linear_Expression_space_dimension (ppl_const_Linear_Expression_t le, ppl_-dimension_type *m)

  Writes to `m` *the space dimension of* `le`.

- int ppl_Linear_Expression_coefficient (ppl_const_Linear_Expression_t le, ppl_dimension_type var, ppl_Coefficient_t n)

  Copies into `n` *the coefficient of variable* `var` *in the linear expression* `le`.

- int ppl_Linear_Expression_inhomogeneous_term (ppl_const_Linear_Expression_t le, ppl_-Coefficient_t n)

  Copies into `n` *the inhomogeneous term of linear expression* `le`.

- int ppl_Linear_Expression_OK (ppl_const_Linear_Expression_t le)

  Returns a positive integer if `le` *is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if* `le` *is broken. Useful for debugging purposes.*

- int ppl_Linear_Expression_is_zero (ppl_const_Linear_Expression_t le)

  Returns `true` *if and only if* `*this` *is* 0.

- int ppl_Linear_Expression_all_homogeneous_terms_are_zero (ppl_const_Linear_Expression_-t le)

  Returns `true` *if and only if all the homogeneous terms of* `*this` *are* 0.

Functions that May Modify the Linear Expression

- int ppl_Linear_Expression_add_to_coefficient (ppl_Linear_Expression_t le, ppl_dimension_type var, ppl_const_Coefficient_t n)

  Adds `n` *to the coefficient of variable* `var` *in the linear expression* `le`*. The space dimension is set to be the maximum between* `var` *+ 1 and the old space dimension.*

- int ppl_Linear_Expression_add_to_inhomogeneous (ppl_Linear_Expression_t le, ppl_const_-Coefficient_t n)

  Adds `n` *to the inhomogeneous term of the linear expression* `le`.

- int ppl_add_Linear_Expression_to_Linear_Expression (ppl_Linear_Expression_t dst, ppl_-const_Linear_Expression_t src)

  Adds the linear expression `src` *to* `dst`.

- int ppl_subtract_Linear_Expression_from_Linear_Expression (ppl_Linear_Expression_t dst, ppl_const_Linear_Expression_t src)

  Subtracts the linear expression `src` *from* `dst`.

- int ppl_multiply_Linear_Expression_by_Coefficient (ppl_Linear_Expression_t le, ppl_const_Coefficient_t n)
  Multiply the linear expression `dst` *by* `n`.

Input/Output Functions

- int ppl_io_print_Linear_Expression (ppl_const_Linear_Expression_t x)
  Prints `x` *to* `stdout`.
- int ppl_io_fprint_Linear_Expression (FILE *stream, ppl_const_Linear_Expression_t x)
  Prints `x` *to the given output* `stream`.
- int ppl_io_asprint_Linear_Expression (char **strp, ppl_const_Linear_Expression_t x)
  Prints `x` *to a malloc-allocated string, a pointer to which is returned via* `strp`.
- int ppl_Linear_Expression_ascii_dump (ppl_const_Linear_Expression_t x, FILE *stream)
  Dumps an ascii representation of `x` *on* `stream`.
- int ppl_Linear_Expression_ascii_load (ppl_Linear_Expression_t x, FILE *stream)
  Loads an ascii representation of `x` *from* `stream`.

7.16.1 Detailed Description

Types and functions for linear expressions. The types and functions for linear expression provide an interface towards *Linear_Expression*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.17 ppl_MIP_Problem_tag Interface Reference

Types and functions for MIP problems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Symbolic Constants

- int PPL_OPTIMIZATION_MODE_MAXIMIZATION
  Code of the "maximization" optimization mode.
- int PPL_OPTIMIZATION_MODE_MINIMIZATION
  Code of the "minimization" optimization mode.
- int PPL_MIP_PROBLEM_STATUS_UNFEASIBLE

Code of the "unfeasible MIP problem" status.

- int PPL_MIP_PROBLEM_STATUS_UNBOUNDED
  Code of the "unbounded MIP problem" status.
- int PPL_MIP_PROBLEM_STATUS_OPTIMIZED
  Code of the "optimized MIP problem" status.
- int PPL_MIP_PROBLEM_CONTROL_PARAMETER_NAME_PRICING
  Code for the MIP problem's "pricing" control parameter name.
- int PPL_MIP_PROBLEM_CONTROL_PARAMETER_PRICING_TEXTBOOK
  Code of MIP problem's "textbook" pricing method.
- int PPL_MIP_PROBLEM_CONTROL_PARAMETER_PRICING_STEEPEST_EDGE_EXACT
  Code of MIP problem's "exact steepest-edge" pricing method.
- int PPL_MIP_PROBLEM_CONTROL_PARAMETER_PRICING_STEEPEST_EDGE_FLOAT
  Code of MIP problem's "float steepest-edge" pricing method.

Constructors, Assignment and Destructor

- int ppl_new_MIP_Problem_from_space_dimension (ppl_MIP_Problem_t *pmip, ppl_dimension_type d)
  Builds a trivial MIP problem of dimension `d` and writes a handle to it at address `pmip`.
- int ppl_new_MIP_Problem (ppl_MIP_Problem_t *pmip, ppl_dimension_type d, ppl_const_Constraint_System_t cs, ppl_const_Linear_Expression_t le, int m)
  Builds a MIP problem of space dimension `d` having feasible region `cs`, objective function `le` and optimization mode `m`; writes a handle to it at address `pmip`.
- int ppl_new_MIP_Problem_from_MIP_Problem (ppl_MIP_Problem_t *pmip, ppl_const_MIP_Problem_t mip)
  Builds a MIP problem that is a copy of `mip`; writes a handle for the newly created system at address `pmip`.
- int ppl_assign_MIP_Problem_from_MIP_Problem (ppl_MIP_Problem_t dst, ppl_const_MIP_Problem_t src)
  Assigns a copy of the MIP problem `src` to `dst`.
- int ppl_delete_MIP_Problem (ppl_const_MIP_Problem_t mip)
  Invalidates the handle `mip`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the MIP_Problem

- int ppl_MIP_Problem_space_dimension (ppl_const_MIP_Problem_t mip, ppl_dimension_type *m)
  Writes to `m` the dimension of the vector space enclosing `mip`.
- int ppl_MIP_Problem_number_of_integer_space_dimensions (ppl_const_MIP_Problem_t mip, ppl_dimension_type *m)

Writes to `m` *the number of integer space dimensions of* `mip`.

- int ppl_MIP_Problem_integer_space_dimensions (ppl_const_MIP_Problem_t mip, ppl_dimension_type ds[ ])

  Writes in the first positions of the array `ds` *all the integer space dimensions of problem* `mip`. *If the array is not big enough to hold all of the integer space dimensions, the behavior is undefined.*

- int ppl_MIP_Problem_number_of_constraints (ppl_const_MIP_Problem_t mip, ppl_dimension_type *m)

  Writes to `m` *the number of constraints defining the feasible region of* `mip`.

- int ppl_MIP_Problem_constraint_at_index (ppl_const_MIP_Problem_t mip, ppl_dimension_type i, ppl_const_Constraint_t *pc)

  Writes at address `pc` *a const handle to the* `i-th` *constraint defining the feasible region of the MIP problem* `mip`.

- int ppl_MIP_Problem_objective_function (ppl_const_MIP_Problem_t mip, ppl_const_Linear_Expression_t *ple)

  Writes a const handle to the linear expression defining the objective function of the MIP problem `mip` *at address* `ple`.

- int ppl_MIP_Problem_optimization_mode (ppl_const_MIP_Problem_t mip)

  Returns the optimization mode of the MIP problem `mip`.

- int ppl_MIP_Problem_OK (ppl_const_MIP_Problem_t mip)

  Returns a positive integer if `mip` *is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if* `mip` *is broken. Useful for debugging purposes.*

Functions that May Modify the MIP_Problem

- int ppl_MIP_Problem_clear (ppl_MIP_Problem_t mip)

  Resets the MIP problem to be a trivial problem of space dimension 0.

- int ppl_MIP_Problem_add_space_dimensions_and_embed (ppl_MIP_Problem_t mip, ppl_dimension_type d)

  Adds `d` *new dimensions to the space enclosing the MIP problem* `mip` *and to* `mip` *itself.*

- int ppl_MIP_Problem_add_to_integer_space_dimensions (ppl_MIP_Problem_t mip, ppl_dimension_type ds[ ], size_t n)

  Sets the space dimensions that are specified in first `n` *positions of the array* `ds` *to be integer dimensions of problem* `mip`. *The presence of duplicates in* `ds` *is a waste but an innocuous one.*

- int ppl_MIP_Problem_add_constraint (ppl_MIP_Problem_t mip, ppl_const_Constraint_t c)

  Modifies the feasible region of the MIP problem `mip` *by adding a copy of the constraint* `c`.

- int ppl_MIP_Problem_add_constraints (ppl_MIP_Problem_t mip, ppl_const_Constraint_System_t cs)

  Modifies the feasible region of the MIP problem `mip` *by adding a copy of the constraints in* `cs`.

- int ppl_MIP_Problem_set_objective_function (ppl_MIP_Problem_t mip, ppl_const_Linear_Expression_t le)

  Sets the objective function of the MIP problem `mip` *to a copy of* `le`.

- int ppl_MIP_Problem_set_optimization_mode (ppl_MIP_Problem_t mip, int mode)
  Sets the optimization mode of the MIP problem `mip` to `mode`.

Computing the Solution of the MIP_Problem

- int ppl_MIP_Problem_is_satisfiable (ppl_const_MIP_Problem_t mip)
  Returns a positive integer if `mip` is satisfiable; returns 0 otherwise.
- int ppl_MIP_Problem_solve (ppl_const_MIP_Problem_t mip)
  Solves the MIP problem `mip`, returning an exit status.
- int ppl_MIP_Problem_evaluate_objective_function (ppl_const_MIP_Problem_t mip, ppl_const_Generator_t g, ppl_Coefficient_t num, ppl_Coefficient_t den)
  Evaluates the objective function of `mip` on point `g`.
- int ppl_MIP_Problem_feasible_point (ppl_const_MIP_Problem_t mip, ppl_const_Generator_t *pg)
  Writes a const handle to a feasible point for the MIP problem `mip` at address `pg`.
- int ppl_MIP_Problem_optimizing_point (ppl_const_MIP_Problem_t mip, ppl_const_Generator_t *pg)
  Writes a const handle to an optimizing point for the MIP problem `mip` at address `pg`.
- int ppl_MIP_Problem_optimal_value (ppl_const_MIP_Problem_t mip, ppl_Coefficient_t num, ppl_Coefficient_t den)
  Returns the optimal value for `mip`.

Querying/Setting Control Parameters

- int ppl_MIP_Problem_get_control_parameter (ppl_const_MIP_Problem_t mip, int name)
  Returns the value of control parameter `name` in problem `mip`.
- int ppl_MIP_Problem_set_control_parameter (ppl_MIP_Problem_t mip, int value)
  Sets control parameter `value` in problem `mip`.
- int ppl_MIP_Problem_total_memory_in_bytes (ppl_const_MIP_Problem_t mip, size_t *sz)
  Writes into `*sz` the size in bytes of the memory occupied by `mip`.
- int ppl_MIP_Problem_external_memory_in_bytes (ppl_const_MIP_Problem_t mip, size_t *sz)
  Writes into `*sz` the size in bytes of the memory managed by `mip`.

Input/Output Functions

- int ppl_io_print_MIP_Problem (ppl_const_MIP_Problem_t x)
  Prints `x` to `stdout`.
- int ppl_io_fprint_MIP_Problem (FILE *stream, ppl_const_MIP_Problem_t x)
  Prints `x` to the given output `stream`.
- int ppl_io_asprint_MIP_Problem (char **strp, ppl_const_MIP_Problem_t x)

Prints `x` *to a malloc-allocated string, a pointer to which is returned via* `strp`.

- int ppl_MIP_Problem_ascii_dump (ppl_const_MIP_Problem_t x, FILE *stream)

  Dumps an ascii representation of `x` *on* `stream`.

- int ppl_MIP_Problem_ascii_load (ppl_MIP_Problem_t x, FILE *stream)

  Loads an ascii representation of `x` *from* `stream`.

7.17.1 Detailed Description

Types and functions for MIP problems. The types and functions for MIP problems provide an interface towards *MIP_Problem*.

7.17.2 Friends And Related Function Documentation

7.17.2.1 int ppl_MIP_Problem_solve (ppl_const_MIP_Problem_t *mip*) [related]

Solves the MIP problem `mip`, returning an exit status.

Returns

`PPL_MIP_PROBLEM_STATUS_UNFEASIBLE` if the MIP problem is not satisfiable; `PPL_MIP_PROBLEM_STATUS_UNBOUNDED` if the MIP problem is satisfiable but there is no finite bound to the value of the objective function; `PPL_MIP_PROBLEM_STATUS_OPTIMIZED` if the MIP problem admits an optimal solution.

7.17.2.2 int ppl_MIP_Problem_evaluate_objective_function (ppl_const_MIP_Problem_t *mip*, ppl_const_Generator_t *g*, ppl_Coefficient_t *num*, ppl_Coefficient_t *den*) [related]

Evaluates the objective function of `mip` on point `g`.

Parameters

mip The MIP problem defining the objective function;

g The generator on which the objective function will be evaluated;

num Will be assigned the numerator of the objective function value;

den Will be assigned the denominator of the objective function value;

7.17.2.3 int ppl_MIP_Problem_optimal_value (ppl_const_MIP_Problem_t *mip*, ppl_Coefficient_t *num*, ppl_Coefficient_t *den*) [related]

Returns the optimal value for `mip`.

Parameters

mip The MIP problem;

num Will be assigned the numerator of the optimal value;

den Will be assigned the denominator of the optimal value.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.18 ppl_PIP_Decision_Node_tag Interface Reference

Types and functions for PIP decision nodes.

`#include <ppl_c_header.h>`

Related Functions

(Note that these are not member functions.)

- int ppl_PIP_Decision_Node_get_child_node (ppl_const_PIP_Decision_Node_t pip_dec, int b, ppl_-const_PIP_Tree_Node_t ∗pip_tree)

  Writes to `pip_tree` a const pointer to either the true branch (if `b` is not zero) or the false branch (if `b` is zero) of `pip_dec`.

Input/Output Functions

- int ppl_io_print_PIP_Decision_Node (ppl_const_PIP_Decision_Node_t x)

  Prints `x` to `stdout`.

- int ppl_io_fprint_PIP_Decision_Node (FILE ∗stream, ppl_const_PIP_Decision_Node_t x)

  Prints `x` to the given output `stream`.

- int ppl_io_asprint_PIP_Decision_Node (char ∗∗strp, ppl_const_PIP_Decision_Node_t x)

  Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.

- int ppl_PIP_Decision_Node_ascii_dump (ppl_const_PIP_Decision_Node_t x, FILE ∗stream)

  Dumps an ascii representation of `x` on `stream`.

- int ppl_PIP_Decision_Node_ascii_load (ppl_PIP_Decision_Node_t x, FILE ∗stream)

  Loads an ascii representation of `x` from `stream`.

7.18.1 Detailed Description

Types and functions for PIP decision nodes. The types and functions for decision nodes provide an interface towards *PIP_Decision_Node*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.19 ppl_PIP_Problem_tag Interface Reference

Types and functions for PIP problems.

`#include <ppl_c_header.h>`

Related Functions

(Note that these are not member functions.)

Symbolic Constants

- int PPL_PIP_PROBLEM_STATUS_UNFEASIBLE
  Code of the "unfeasible PIP problem" status.
- int PPL_PIP_PROBLEM_STATUS_OPTIMIZED
  Code of the "optimized PIP problem" status.
- int PPL_PIP_PROBLEM_CONTROL_PARAMETER_NAME_CUTTING_STRATEGY
  Code for the PIP problem's "cutting strategy" control parameter name.
- int PPL_PIP_PROBLEM_CONTROL_PARAMETER_NAME_PIVOT_ROW_STRATEGY
  Code for the PIP problem's "pivot row strategy" control parameter name.
- int PPL_PIP_PROBLEM_CONTROL_PARAMETER_CUTTING_STRATEGY_FIRST
  Code of PIP problem's "first" cutting strategy.
- int PPL_PIP_PROBLEM_CONTROL_PARAMETER_CUTTING_STRATEGY_DEEPEST
  Code of PIP problem's "deepest" cutting strategy.
- int PPL_PIP_PROBLEM_CONTROL_PARAMETER_CUTTING_STRATEGY_ALL
  Code of PIP problem's "all" cutting strategy.
- int PPL_PIP_PROBLEM_CONTROL_PARAMETER_PIVOT_ROW_STRATEGY_FIRST
  Code of PIP problem's "first" pivot row strategy.
- int PPL_PIP_PROBLEM_CONTROL_PARAMETER_PIVOT_ROW_STRATEGY_MAX_-COLUMN
  Code of PIP problem's "max column" pivot row strategy.

Constructors, Assignment and Destructor

- int ppl_new_PIP_Problem_from_space_dimension (ppl_PIP_Problem_t *ppip, ppl_dimension_-type d)
  Builds a trivial PIP problem of dimension `d` and writes a handle to it at address `ppip`.
- int ppl_new_PIP_Problem_from_PIP_Problem (ppl_PIP_Problem_t *ppip, ppl_const_PIP_-Problem_t pip)
  Builds a PIP problem that is a copy of `pip`; writes a handle for the newly created problem at address `ppip`.
- int ppl_assign_PIP_Problem_from_PIP_Problem (ppl_PIP_Problem_t dst, ppl_const_PIP_-Problem_t src)

Assigns a copy of the PIP problem `src` to `dst`.

- int ppl_new_PIP_Problem_from_constraints (ppl_PIP_Problem_t *ppip, ppl_dimension_type d, ppl_Constraint_System_const_iterator_t first, ppl_Constraint_System_const_iterator_t last, size_t n, ppl_dimension_type ds[ ])

  Builds a PIP problem having space dimension `d` from the sequence of constraints in the range [first, last)*; the `n` dimensions whose indices occur in `ds` are interpreted as parameters.*

- int ppl_delete_PIP_Problem (ppl_const_PIP_Problem_t pip)

  Invalidates the handle `pip`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the PIP_Problem

- int ppl_PIP_Problem_space_dimension (ppl_const_PIP_Problem_t pip, ppl_dimension_type *m)

  Writes to `m` the dimension of the vector space enclosing `pip`.

- int ppl_PIP_Problem_number_of_parameter_space_dimensions (ppl_const_PIP_Problem_t pip, ppl_dimension_type *m)

  Writes to `m` the number of parameter space dimensions of `pip`.

- int ppl_PIP_Problem_parameter_space_dimensions (ppl_const_PIP_Problem_t pip, ppl_-dimension_type ds[ ])

  Writes in the first positions of the array `ds` all the parameter space dimensions of problem `pip`. If the array is not big enough to hold all of the parameter space dimensions, the behavior is undefined.

- int ppl_PIP_Problem_get_big_parameter_dimension (ppl_const_PIP_Problem_t pip, ppl_-dimension_type *pd)

  Writes into `*pd` the big parameter dimension of PIP problem `pip`.

- int ppl_PIP_Problem_number_of_constraints (ppl_const_PIP_Problem_t pip, ppl_dimension_-type *m)

  Writes to `m` the number of constraints defining the feasible region of `pip`.

- int ppl_PIP_Problem_constraint_at_index (ppl_const_PIP_Problem_t pip, ppl_dimension_type i, ppl_const_Constraint_t *pc)

  Writes at address `pc` a const handle to the `i-th` constraint defining the feasible region of the PIP problem `pip`.

- int ppl_PIP_Problem_total_memory_in_bytes (ppl_const_PIP_Problem_t pip, size_t *sz)

  Writes into `*sz` the size in bytes of the memory occupied by `pip`.

- int ppl_PIP_Problem_external_memory_in_bytes (ppl_const_PIP_Problem_t pip, size_t *sz)

  Writes into `*sz` the size in bytes of the memory managed by `pip`.

- int ppl_PIP_Problem_OK (ppl_const_PIP_Problem_t pip)

  Returns a positive integer if `pip` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `pip` is broken. Useful for debugging purposes.

Functions that May Modify the PIP_Problem

- int ppl_PIP_Problem_clear (ppl_PIP_Problem_t pip)

Resets the PIP problem to be a trivial problem of space dimension 0.

- int ppl_PIP_Problem_add_space_dimensions_and_embed (ppl_PIP_Problem_t pip, ppl_dimension_type pip_vars, ppl_dimension_type pip_params)

  Adds `pip_vars + pip_params` new space dimensions and embeds the PIP problem `pip` in the new vector space.

- int ppl_PIP_Problem_add_to_parameter_space_dimensions (ppl_PIP_Problem_t pip, ppl_dimension_type ds[ ], size_t n)

  Sets the space dimensions that are specified in first `n` positions of the array `ds` to be parameter dimensions of problem `pip`. The presence of duplicates in `ds` is a waste but an innocuous one.

- int ppl_PIP_Problem_set_big_parameter_dimension (ppl_PIP_Problem_t pip, ppl_dimension_type d)

  Sets the big parameter dimension of PIP problem `pip` to `d`.

- int ppl_PIP_Problem_add_constraint (ppl_PIP_Problem_t pip, ppl_const_Constraint_t c)

  Modifies the feasible region of the PIP problem `pip` by adding a copy of the constraint `c`.

- int ppl_PIP_Problem_add_constraints (ppl_PIP_Problem_t pip, ppl_const_Constraint_System_t cs)

  Modifies the feasible region of the PIP problem `pip` by adding a copy of the constraints in `cs`.

Computing and Printing the Solution of the PIP_Problem

- int ppl_PIP_Problem_is_satisfiable (ppl_const_PIP_Problem_t pip)

  Returns a positive integer if `pip` is satisfiable and an optimal solution can be found; returns 0 otherwise.

- int ppl_PIP_Problem_solve (ppl_const_PIP_Problem_t pip)

  Solves the PIP problem `pip`, returning an exit status.

- int ppl_PIP_Problem_solution (ppl_const_PIP_Problem_t pip, ppl_const_PIP_Tree_Node_t *pip_tree)

  Writes to `pip_tree` a solution for `pip`, if it exists.

- int ppl_PIP_Problem_optimizing_solution (ppl_const_PIP_Problem_t pip, ppl_const_PIP_Tree_Node_t *pip_tree)

  Writes to `pip_tree` an optimizing solution for `pip`, if it exists.

Querying/Setting Control Parameters

- int ppl_PIP_Problem_get_control_parameter (ppl_const_PIP_Problem_t pip, int name)

  Returns the value of control parameter `name` in problem `pip`.

- int ppl_PIP_Problem_set_control_parameter (ppl_PIP_Problem_t pip, int value)

  Sets control parameter `value` in problem `pip`.

Input/Output Functions

- int ppl_io_print_PIP_Problem (ppl_const_PIP_Problem_t x)

  Prints `x` to `stdout`.

- int ppl_io_fprint_PIP_Problem (FILE *stream, ppl_const_PIP_Problem_t x)

  Prints `x` *to the given output* `stream`.

- int ppl_io_asprint_PIP_Problem (char **strp, ppl_const_PIP_Problem_t x)

  Prints `x` *to a malloc-allocated string, a pointer to which is returned via* `strp`.

- int ppl_PIP_Problem_ascii_dump (ppl_const_PIP_Problem_t x, FILE *stream)

  Dumps an ascii representation of `x` *on* `stream`.

- int ppl_PIP_Problem_ascii_load (ppl_PIP_Problem_t x, FILE *stream)

  Loads an ascii representation of `x` *from* `stream`.

7.19.1 Detailed Description

Types and functions for PIP problems. The types and functions for PIP problems provide an interface towards *PIP_Problem*.

7.19.2 Friends And Related Function Documentation

7.19.2.1 int ppl_PIP_Problem_space_dimension (ppl_const_PIP_Problem_t *pip*, ppl_dimension_type * *m*) [related]

Writes to `m` the dimension of the vector space enclosing `pip`.

The vector space dimensions includes both the problem variables and the problem parameters, but they do not include the artificial parameters.

7.19.2.2 int ppl_PIP_Problem_add_space_dimensions_and_embed (ppl_PIP_Problem_t *pip*, ppl_dimension_type *pip_vars*, ppl_dimension_type *pip_params*) [related]

Adds `pip_vars + pip_params` new space dimensions and embeds the PIP problem `pip` in the new vector space.

Parameters

pip The PIP problem to be embedded in the new vector space.

pip_vars The number of space dimensions to add that are interpreted as PIP problem variables (i.e., non parameters). These are added *before* adding the `pip_params` parameters.

pip_params The number of space dimensions to add that are interpreted as PIP problem parameters. These are added *after* having added the `pip_vars` problem variables.

The new space dimensions will be those having the highest indexes in the new PIP problem; they are initially unconstrained.

7.19.2.3 int ppl_PIP_Problem_solve (ppl_const_PIP_Problem_t *pip*) [related]

Solves the PIP problem `pip`, returning an exit status.

Returns

`PPL_PIP_PROBLEM_STATUS_UNFEASIBLE` if the PIP problem is not satisfiable; `PPL_PIP_PROBLEM_STATUS_OPTIMIZED` if the PIP problem admits an optimal solution.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.20 ppl_PIP_Solution_Node_tag Interface Reference

Types and functions for PIP solution nodes.

`#include <ppl_c_header.h>`

Related Functions

(Note that these are not member functions.)

- int ppl_PIP_Solution_Node_get_parametric_values (ppl_const_PIP_Solution_Node_t pip_sol, ppl_dimension_type var, ppl_const_Linear_Expression_t *le)

  Writes to `le` a const pointer to the parametric expression of the values of variable `var` in solution node `pip_sol`.

Input/Output Functions

- int ppl_io_print_PIP_Solution_Node (ppl_const_PIP_Solution_Node_t x)

  Prints `x` to `stdout`.

- int ppl_io_fprint_PIP_Solution_Node (FILE *stream, ppl_const_PIP_Solution_Node_t x)

  Prints `x` to the given output `stream`.

- int ppl_io_asprint_PIP_Solution_Node (char **strp, ppl_const_PIP_Solution_Node_t x)

  Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.

- int ppl_PIP_Solution_Node_ascii_dump (ppl_const_PIP_Solution_Node_t x, FILE *stream)

  Dumps an ascii representation of `x` on `stream`.

- int ppl_PIP_Solution_Node_ascii_load (ppl_PIP_Solution_Node_t x, FILE *stream)

  Loads an ascii representation of `x` from `stream`.

7.20.1 Detailed Description

Types and functions for PIP solution nodes. The types and functions for solution nodes provide an interface towards *PIP_Solution_Node*.

7.20.2 Friends And Related Function Documentation

7.20.2.1 int ppl_PIP_Solution_Node_get_parametric_values (ppl_const_PIP_Solution_Node_t *pip_sol*, ppl_dimension_type *var*, ppl_const_Linear_Expression_t * *le*) [related]

Writes to `le` a const pointer to the parametric expression of the values of variable `var` in solution node `pip_sol`.

The linear expression assigned to `le` will only refer to (problem or artificial) parameters.

Parameters

pip_sol The solution tree node.

var The variable which is queried about.

le The returned expression for variable `var`.

Returns

PPL_ERROR_INVALID_ARGUMENT Returned if `var` is dimension-incompatible with `*this` or if `var` is a problem parameter.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.21 ppl_PIP_Tree_Node_tag Interface Reference

Types and functions for generic PIP tree nodes.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

- int ppl_PIP_Tree_Node_as_solution (ppl_const_PIP_Tree_Node_t spip_tree, ppl_const_PIP_Solution_Node_t *dpip_tree)

  Writes to `dpip_tree` the solution node if `spip_tree` is a solution node, and 0 otherwise.

- int ppl_PIP_Tree_Node_as_decision (ppl_const_PIP_Tree_Node_t spip_tree, ppl_const_PIP_Decision_Node_t *dpip_tree)

  Writes to `dpip_tree` the decision node if `spip_tree` is a decision node, and 0 otherwise.

- int ppl_PIP_Tree_Node_get_constraints (ppl_const_PIP_Tree_Node_t pip_tree, ppl_const_Constraint_System_t *pcs)

  Writes to `pcs` the local system of parameter constraints at the pip tree node `pip_tree`.

- int ppl_PIP_Tree_Node_OK (ppl_const_PIP_Tree_Node_t pip)

  Returns a positive integer if `pip_tree` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `pip_tree` is broken. Useful for debugging purposes.

- int ppl_PIP_Tree_Node_number_of_artificials (ppl_const_PIP_Tree_Node_t pip_tree, ppl_-dimension_type *m)

  Writes to `m` *the number of elements in the artificial parameter sequence in the pip tree node* `pip_tree`.

- int ppl_PIP_Tree_Node_begin (ppl_const_PIP_Tree_Node_t pip_tree, ppl_Artificial_Parameter_-Sequence_const_iterator_t pit)

  Assigns to `pit` *a const iterator "pointing" to the beginning of the artificial parameter sequence in the pip tree node* `pip_tree`.

- int ppl_PIP_Tree_Node_end (ppl_const_PIP_Tree_Node_t pip_tree, ppl_Artificial_Parameter_-Sequence_const_iterator_t pit)

  Assigns to `pit` *a const iterator "pointing" to the end of the artificial parameter sequence in the pip tree node* `pip_tree`.

Input/Output Functions

- int ppl_io_print_PIP_Tree_Node (ppl_const_PIP_Tree_Node_t x)

  Prints `x` *to* `stdout`.

- int ppl_io_fprint_PIP_Tree_Node (FILE *stream, ppl_const_PIP_Tree_Node_t x)

  Prints `x` *to the given output* `stream`.

- int ppl_io_asprint_PIP_Tree_Node (char **strp, ppl_const_PIP_Tree_Node_t x)

  Prints `x` *to a malloc-allocated string, a pointer to which is returned via* `strp`.

- int ppl_PIP_Tree_Node_ascii_dump (ppl_const_PIP_Tree_Node_t x, FILE *stream)

  Dumps an ascii representation of `x` *on* `stream`.

- int ppl_PIP_Tree_Node_ascii_load (ppl_PIP_Tree_Node_t x, FILE *stream)

  Loads an ascii representation of `x` *from* `stream`.

7.21.1 Detailed Description

Types and functions for generic PIP tree nodes. The types and functions for tree nodes provide an interface towards *PIP_Tree_Node*.

The documentation for this interface was generated from the following file:

- ppl_c_header.h

7.22 ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag Interface Reference

Types and functions for iterating on the disjuncts of a const ppl_Pointset_Powerset_C_Polyhedron_tag.

Related Functions

(Note that these are not member functions.)

Construction, Initialization and Destruction

- int ppl_new_Pointset_Powerset_C_Polyhedron_const_iterator (ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t *pit)

  Builds a new 'const iterator' and writes a handle to it at address `pit`.

- int ppl_new_Pointset_Powerset_C_Polyhedron_const_iterator_from_const_iterator (ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t *pit, ppl_const_Pointset_Powerset_C_Polyhedron_const_iterator_t y)

  Builds a copy of `y` *and writes a handle to it at address* `pit`.

- int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_begin (ppl_const_Pointset_Powerset_C_Polyhedron_t ps, ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t psit)

  Assigns to `psit` *a const iterator "pointing" to the beginning of the sequence of disjuncts of* `ps`.

- int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_end (ppl_const_Pointset_Powerset_C_Polyhedron_t ps, ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t psit)

  Assigns to `psit` *a const iterator "pointing" past the end of the sequence of disjuncts of* `ps`.

- int ppl_delete_Pointset_Powerset_C_Polyhedron_const_iterator (ppl_const_Pointset_Powerset_C_Polyhedron_const_iterator_t it)

  Invalidates the handle `it`*: this makes sure the corresponding resources will eventually be released.*

Dereferencing, Increment, Decrement and Equality Testing

- int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_dereference (ppl_const_Pointset_Powerset_C_Polyhedron_const_iterator_t it, ppl_const_Polyhedron_t *d)

  Dereferences `it` *writing a const handle to the resulting disjunct at address* `d`.

- int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_increment (ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t it)

  Increments `it` *so that it "points" to the next disjunct.*

- int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_decrement (ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t it)

  Decrements `it` *so that it "points" to the previous disjunct.*

- int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_equal_test (ppl_const_Pointset_Powerset_C_Polyhedron_const_iterator_t x, ppl_const_Pointset_Powerset_C_Polyhedron_const_iterator_t y)

  Returns a positive integer if the iterators corresponding to `x` *and* `y` *are equal; returns 0 if they are different.*

7.22.1 Detailed Description

Types and functions for iterating on the disjuncts of a const ppl_Pointset_Powerset_C_Polyhedron_tag.

7.22.2 Friends And Related Function Documentation

7.22.2.1 int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_dereference (ppl_const_-Pointset_Powerset_C_Polyhedron_const_iterator_t *it*, ppl_const_Polyhedron_t ∗ *d*) [related]

Dereferences `it` writing a const handle to the resulting disjunct at address `d`.

Warning

On exit, the disjunct `d` is still owned by the powerset object: any function call on the owning powerset object may invalidate it. Moreover, `d` should **not** be deleted directly: its resources will be released when deleting the owning powerset.

The documentation for this interface was generated from the following file:

- C_interface.dox

7.23 ppl_Pointset_Powerset_C_Polyhedron_iterator_tag Interface Reference

Types and functions for iterating on the disjuncts of a ppl_Pointset_Powerset_C_Polyhedron_tag.

Related Functions

(Note that these are not member functions.)

Construction, Initialization and Destruction

- int ppl_new_Pointset_Powerset_C_Polyhedron_iterator (ppl_Pointset_Powerset_C_-Polyhedron_iterator_t ∗pit)

  Builds a new 'iterator' and writes a handle to it at address `pit`.

- int ppl_new_Pointset_Powerset_C_Polyhedron_iterator_from_iterator (ppl_Pointset_Powerset_-C_Polyhedron_iterator_t ∗pit, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t y)

  Builds a copy of `y` and writes a handle to it at address `pit`.

- int ppl_Pointset_Powerset_C_Polyhedron_iterator_begin (ppl_Pointset_Powerset_C_-Polyhedron_t ps, ppl_Pointset_Powerset_C_Polyhedron_iterator_t psit)

  Assigns to `psit` an iterator "pointing" to the beginning of the sequence of disjuncts of `ps`.

- int ppl_Pointset_Powerset_C_Polyhedron_iterator_end (ppl_Pointset_Powerset_C_Polyhedron_t ps, ppl_Pointset_Powerset_C_Polyhedron_iterator_t psit)

  Assigns to `psit` an iterator "pointing" past the end of the sequence of disjuncts of `ps`.

- int ppl_delete_Pointset_Powerset_C_Polyhedron_iterator (ppl_const_Pointset_Powerset_C_-Polyhedron_iterator_t it)

  Invalidates the handle `it`: this makes sure the corresponding resources will eventually be released.

Dereferencing, Increment, Decrement and Equality Testing

- int ppl_Pointset_Powerset_C_Polyhedron_iterator_dereference (ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t it, ppl_const_Polyhedron_t *d)

  Dereferences `it` writing a const handle to the resulting disjunct at address `d`.

- int ppl_Pointset_Powerset_C_Polyhedron_iterator_increment (ppl_Pointset_Powerset_C_Polyhedron_iterator_t it)

  Increments `it` so that it "points" to the next disjunct.

- int ppl_Pointset_Powerset_C_Polyhedron_iterator_decrement (ppl_Pointset_Powerset_C_Polyhedron_iterator_t it)

  Decrements `it` so that it "points" to the previous disjunct.

- int ppl_Pointset_Powerset_C_Polyhedron_iterator_equal_test (ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t x, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t y)

  Returns a positive integer if the iterators corresponding to `x` and `y` are equal; returns 0 if they are different.

7.23.1 Detailed Description

Types and functions for iterating on the disjuncts of a ppl_Pointset_Powerset_C_Polyhedron_tag.

7.23.2 Friends And Related Function Documentation

7.23.2.1 int ppl_Pointset_Powerset_C_Polyhedron_iterator_dereference (ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t *it*, ppl_const_Polyhedron_t * *d*) `[related]`

Dereferences `it` writing a const handle to the resulting disjunct at address `d`.

Note

Even though `it` is an non-const iterator, dereferencing it results in a handle to a **const** disjunct. This is because mutable iterators are meant to allow for the modification of the sequence of disjuncts (e.g., by dropping elements), while preventing direct modifications of the disjuncts they point to.

Warning

On exit, the disjunct `d` is still owned by the powerset object: any function call on the owning powerset object may invalidate it. Moreover, `d` should **not** be deleted directly: its resources will be released when deleting the owning powerset.

The documentation for this interface was generated from the following file:

- C_interface.dox

7.24 ppl_Pointset_Powerset_C_Polyhedron_tag Interface Reference

Types and functions for the Pointset_Powerset of C_Polyhedron objects.

Related Functions

(Note that these are not member functions.)

Ad Hoc Functions for Pointset_Powerset domains

- int ppl_Pointset_Powerset_C_Polyhedron_omega_reduce (ppl_const_Pointset_Powerset_C_Polyhedron_t ps)

  Drops from the sequence of disjuncts in `ps` all the non-maximal elements so that `ps` is non-redundant.

- int ppl_Pointset_Powerset_C_Polyhedron_size (ppl_const_Pointset_Powerset_C_Polyhedron_t ps, size_t *sz)

  Writes to `sz` the number of disjuncts in `ps`.

- int ppl_Pointset_Powerset_C_Polyhedron_geometrically_covers_Pointset_Powerset_C_Polyhedron (ppl_const_Pointset_Powerset_C_Polyhedron_t x, ppl_const_Pointset_Powerset_C_Polyhedron_t y)

  Returns a positive integer if powerset `x` geometrically covers powerset `y`; returns 0 otherwise.

- int ppl_Pointset_Powerset_C_Polyhedron_geometrically_equals_Pointset_Powerset_C_Polyhedron (ppl_const_Pointset_Powerset_C_Polyhedron_t x, ppl_const_Pointset_Powerset_C_Polyhedron_t y)

  Returns a positive integer if powerset `x` is geometrically equal to powerset `y`; returns 0 otherwise.

- int ppl_Pointset_Powerset_C_Polyhedron_add_disjunct (ppl_Pointset_Powerset_C_Polyhedron_t ps, ppl_const_Polyhedron_t d)

  Adds to `ps` a copy of disjunct `d`.

- int ppl_Pointset_Powerset_C_Polyhedron_drop_disjunct (ppl_Pointset_Powerset_C_Polyhedron_t ps, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t cit, ppl_Pointset_Powerset_C_Polyhedron_iterator_t it)

  Drops from `ps` the disjunct pointed to by `cit`, assigning to `it` an iterator to the disjunct following `cit`.

- int ppl_Pointset_Powerset_C_Polyhedron_drop_disjuncts (ppl_Pointset_Powerset_C_Polyhedron_t ps, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t first, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t last)

  Drops from `ps` all the disjuncts from `first` to `last` (excluded).

- int ppl_Pointset_Powerset_C_Polyhedron_pairwise_reduce (ppl_Pointset_Powerset_C_Polyhedron_t ps)

  Modifies `ps` by (recursively) merging together the pairs of disjuncts whose upper-bound is the same as their set-theoretical union.

7.24.1 Detailed Description

Types and functions for the Pointset_Powerset of C_Polyhedron objects. The powerset domains can be instantiated by taking as a base domain any fixed semantic geometric description (C and NNC polyhedra, BD and octagonal shapes, boxes and grids). An element of the powerset domain represents a disjunctive collection of base objects (its disjuncts), all having the same space dimension.

Besides the functions that are available in all semantic geometric descriptions (whose documentation is not repeated here), the powerset domain also provides several ad hoc functions. In particular, the iterator types allow for the examination and manipulation of the collection of disjuncts.

7.24.2 Friends And Related Function Documentation

7.24.2.1 int ppl_Pointset_Powerset_C_Polyhedron_size (ppl_const_Pointset_Powerset_C_-Polyhedron_t *ps*, size_t * *sz*) [related]

Writes to `sz` the number of disjuncts in `ps`.

Note

If present, Omega-redundant elements will be counted too.

The documentation for this interface was generated from the following file:

- C_interface.dox

7.25 ppl_Polyhedron_tag Interface Reference

Types and functions for the domains of C and NNC convex polyhedra.

Related Functions

(Note that these are not member functions.)

Constructors and Assignment for C_Polyhedron

- int ppl_new_C_Polyhedron_from_space_dimension (ppl_Polyhedron_t *pph, ppl_dimension_-type d, int empty)

  Builds a C polyhedron of dimension `d` and writes an handle to it at address `pph`. If `empty` is different from zero, the newly created polyhedron will be empty; otherwise, it will be a universe polyhedron.

- int ppl_new_C_Polyhedron_from_C_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_-Polyhedron_t ph)

  Builds a C polyhedron that is a copy of `ph`; writes a handle for the newly created polyhedron at address `pph`.

- int ppl_new_C_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)

  Builds a C polyhedron that is a copy of `ph`; writes a handle for the newly created polyhedron at address `pph`.

- int ppl_new_C_Polyhedron_from_Constraint_System (ppl_Polyhedron_t *pph, ppl_const_-Constraint_System_t cs)

  Builds a new C polyhedron from the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.

- int ppl_new_C_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t *pph, ppl_-Constraint_System_t cs)

  Builds a new C polyhedron recycling the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.

- int ppl_new_C_Polyhedron_from_Congruence_System (ppl_Polyhedron_t *pph, ppl_const_-Congruence_System_t cs)

Builds a new C polyhedron from the system of congruences `cs` *and writes a handle for the newly created polyhedron at address* `pph`.

- int ppl_new_C_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t *pph, ppl_Congruence_System_t cs)

  Builds a new C polyhedron recycling the system of congruences `cs` *and writes a handle for the newly created polyhedron at address* `pph`.

- int ppl_assign_C_Polyhedron_from_C_Polyhedron (ppl_Polyhedron_t dst, ppl_const_Polyhedron_t src)

  Assigns a copy of the C polyhedron `src` *to the C polyhedron* `dst`.

Constructors and Assignment for NNC_Polyhedron

- int ppl_new_NNC_Polyhedron_from_space_dimension (ppl_Polyhedron_t *pph, ppl_dimension_type d, int empty)

  Builds an NNC polyhedron of dimension `d` *and writes an handle to it at address* `pph`. *If* `empty` *is different from zero, the newly created polyhedron will be empty; otherwise, it will be a universe polyhedron.*

- int ppl_new_NNC_Polyhedron_from_NNC_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph)

  Builds an NNC polyhedron that is a copy of `ph`*; writes a handle for the newly created polyhedron at address* `pph`.

- int ppl_new_NNC_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)

  Builds an NNC polyhedron that is a copy of `ph`*; writes a handle for the newly created polyhedron at address* `pph`.

- int ppl_new_NNC_Polyhedron_from_Constraint_System (ppl_Polyhedron_t *pph, ppl_const_Constraint_System_t cs)

  Builds a new NNC polyhedron from the system of constraints `cs` *and writes a handle for the newly created polyhedron at address* `pph`.

- int ppl_new_NNC_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t *pph, ppl_Constraint_System_t cs)

  Builds a new NNC polyhedron recycling the system of constraints `cs` *and writes a handle for the newly created polyhedron at address* `pph`.

- int ppl_new_NNC_Polyhedron_from_Congruence_System (ppl_Polyhedron_t *pph, ppl_const_Congruence_System_t cs)

  Builds a new NNC polyhedron from the system of congruences `cs` *and writes a handle for the newly created polyhedron at address* `pph`.

- int ppl_new_NNC_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t *pph, ppl_Congruence_System_t cs)

  Builds a new NNC polyhedron recycling the system of congruences `cs` *and writes a handle for the newly created polyhedron at address* `pph`.

- int ppl_assign_NNC_Polyhedron_from_NNC_Polyhedron (ppl_Polyhedron_t dst, ppl_const_Polyhedron_t src)

  Assigns a copy of the NNC polyhedron `src` *to the NNC polyhedron* `dst`.

Constructors Behaving as Conversion Operators

Besides the conversions listed here below, the library also provides conversion operators that build a semantic geometric description starting from ***any*** *other semantic geometric description (e.g., ppl_new_Grid_from_C_Polyhedron, ppl_new_C_Polyhedron_from_BD_Shape_mpq_class, etc.). Clearly, the conversion operators are only available if both the source and the target semantic geometric descriptions have been enabled when configuring the library. The conversions also taking as argument a complexity class sometimes provide non-trivial precision/efficiency trade-offs.*

- int ppl_new_C_Polyhedron_from_NNC_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph)

  Builds a C polyhedron that is a copy of the topological closure of the NNC polyhedron `ph`; writes a handle for the newly created polyhedron at address `pph`.

- int ppl_new_C_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)

  Builds a C polyhedron that approximates NNC_Polyhedron `ph`, using an algorithm whose complexity does not exceed `complexity`; writes a handle for the newly created polyhedron at address `pph`.

- int ppl_new_NNC_Polyhedron_from_C_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph)

  Builds an NNC polyhedron that is a copy of the C polyhedron `ph`; writes a handle for the newly created polyhedron at address `pph`.

- int ppl_new_NNC_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)

  Builds an NNC polyhedron that approximates C_Polyhedron `ph`, using an algorithm whose complexity does not exceed `complexity`; writes a handle for the newly created polyhedron at address `pph`.

Destructor for (C or NNC) Polyhedra

- int ppl_delete_Polyhedron (ppl_const_Polyhedron_t ph)

  Invalidates the handle `ph`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Polyhedron

- int ppl_Polyhedron_space_dimension (ppl_const_Polyhedron_t ph, ppl_dimension_type *m)

  Writes to `m` the dimension of the vector space enclosing `ph`.

- int ppl_Polyhedron_affine_dimension (ppl_const_Polyhedron_t ph, ppl_dimension_type *m)

  Writes to `m` the affine dimension of `ph` (not to be confused with the dimension of its enclosing vector space) or 0, if `ph` is empty.

- int ppl_Polyhedron_relation_with_Constraint (ppl_const_Polyhedron_t ph, ppl_const_Constraint_t c)

  Checks the relation between the polyhedron `ph` and the constraint `c`.

- int ppl_Polyhedron_relation_with_Generator (ppl_const_Polyhedron_t ph, ppl_const_Generator_t g)

  Checks the relation between the polyhedron `ph` and the generator `g`.

- int ppl_Polyhedron_get_constraints (ppl_const_Polyhedron_t ph, ppl_const_Constraint_System_t *pcs)

Writes a const handle to the constraint system defining the polyhedron `ph` *at address* `pcs`*.*

- int ppl_Polyhedron_get_congruences (ppl_const_Polyhedron_t ph, ppl_const_Congruence_System_t *pcs)

  Writes at address `pcs` *a const handle to a system of congruences approximating the polyhedron* `ph`*.*

- int ppl_Polyhedron_get_minimized_constraints (ppl_const_Polyhedron_t ph, ppl_const_Constraint_System_t *pcs)

  Writes a const handle to the minimized constraint system defining the polyhedron `ph` *at address* `pcs`*.*

- int ppl_Polyhedron_get_minimized_congruences (ppl_const_Polyhedron_t ph, ppl_const_Congruence_System_t *pcs)

  Writes at address `pcs` *a const handle to a system of minimized congruences approximating the polyhedron* `ph`*.*

- int ppl_Polyhedron_is_empty (ppl_const_Polyhedron_t ph)

  Returns a positive integer if `ph` *is empty; returns 0 if* `ph` *is not empty.*

- int ppl_Polyhedron_is_universe (ppl_const_Polyhedron_t ph)

  Returns a positive integer if `ph` *is a universe polyhedron; returns 0 if it is not.*

- int ppl_Polyhedron_is_bounded (ppl_const_Polyhedron_t ph)

  Returns a positive integer if `ph` *is bounded; returns 0 if* `ph` *is unbounded.*

- int ppl_Polyhedron_contains_integer_point (ppl_const_Polyhedron_t ph)

  Returns a positive integer if `ph` *contains at least one integer point; returns 0 otherwise.*

- int ppl_Polyhedron_is_topologically_closed (ppl_const_Polyhedron_t ph)

  Returns a positive integer if `ph` *is topologically closed; returns 0 if* `ph` *is not topologically closed.*

- int ppl_Polyhedron_is_discrete (ppl_const_Polyhedron_t ph)

  Returns a positive integer if `ph` *is a discrete set; returns 0 if* `ph` *is not a discrete set.*

- int ppl_Polyhedron_constrains (ppl_Polyhedron_t ph, ppl_dimension_type var)

  Returns a positive integer if `ph` *constrains* `var`*; returns 0 if* `ph` *does not constrain* `var`*.*

- int ppl_Polyhedron_bounds_from_above (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le)

  Returns a positive integer if `le` *is bounded from above in* `ph`*; returns 0 otherwise.*

- int ppl_Polyhedron_bounds_from_below (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le)

  Returns a positive integer if `le` *is bounded from below in* `ph`*; returns 0 otherwise.*

- int ppl_Polyhedron_maximize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le, ppl_Coefficient_t sup_n, ppl_Coefficient_t sup_d, int *pmaximum, ppl_Generator_t point)

  Returns a positive integer if `ph` *is not empty and* `le` *is bounded from above in* `ph`*, in which case the supremum value and a point where* `le` *reaches it are computed.*

- int ppl_Polyhedron_maximize (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le, ppl_Coefficient_t sup_n, ppl_Coefficient_t sup_d, int *pmaximum)

  The same as ppl_Polyhedron_maximize_with_point, but without the output argument for the location where the supremum value is reached.

- int ppl_Polyhedron_minimize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le, ppl_Coefficient_t inf_n, ppl_Coefficient_t inf_d, int *pminimum, ppl_Generator_t point)

  Returns a positive integer if `ph` is not empty and `le` is bounded from below in `ph`, in which case the infimum value and a point where `le` reaches it are computed.

- int ppl_Polyhedron_minimize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le, ppl_Coefficient_t inf_n, ppl_Coefficient_t inf_d, int *pminimum)

  The same as ppl_Polyhedron_minimize_with_point, but without the output argument for the location where the infimum value is reached.

- int ppl_Polyhedron_contains_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron_t y)

  Returns a positive integer if `x` contains or is equal to `y`; returns 0 if it does not.

- int ppl_Polyhedron_strictly_contains_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron_t y)

  Returns a positive integer if `x` strictly contains `y`; returns 0 if it does not.

- int ppl_Polyhedron_is_disjoint_from_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron_t y)

  Returns a positive integer if `x` and `y` are disjoint; returns 0 if they are not.

- int ppl_Polyhedron_equals_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron_t y)

  Returns a positive integer if `x` and `y` are the same polyhedron; returns 0 if they are different.

- int ppl_Polyhedron_OK (ppl_const_Polyhedron_t ph)

  Returns a positive integer if `ph` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `ph` is broken. Useful for debugging purposes.

- int ppl_Polyhedron_external_memory_in_bytes (ppl_const_Polyhedron_t ph, size_t *sz)

  Writes to `sz` a lower bound to the size in bytes of the memory managed by `ph`.

- int ppl_Polyhedron_total_memory_in_bytes (ppl_const_Polyhedron_t ph, size_t *sz)

  Writes to `sz` a lower bound to the size in bytes of the memory managed by `ph`.

Space Dimension Preserving Functions that May Modify the Polyhedron

- int ppl_Polyhedron_add_constraint (ppl_Polyhedron_t ph, ppl_const_Constraint_t c)

  Adds a copy of the constraint `c` to the system of constraints of `ph`.

- int ppl_Polyhedron_add_congruence (ppl_Polyhedron_t ph, ppl_const_Congruence_t c)

  Adds a copy of the congruence `c` to polyhedron of `ph`.

- int ppl_Polyhedron_add_constraints (ppl_Polyhedron_t ph, ppl_const_Constraint_System_t cs)

  Adds a copy of the system of constraints `cs` to the system of constraints of `ph`.

- int ppl_Polyhedron_add_congruences (ppl_Polyhedron_t ph, ppl_const_Congruence_System_t cs)

  Adds a copy of the system of congruences `cs` to the polyhedron `ph`.

- int ppl_Polyhedron_add_recycled_constraints (ppl_Polyhedron_t ph, ppl_Constraint_System_-t cs)

  Adds the system of constraints `cs` to the system of constraints of `ph`.

- int ppl_Polyhedron_add_recycled_congruences (ppl_Polyhedron_t ph, ppl_Congruence_-System_t cs)

  Adds the system of congruences `cs` to the polyhedron `ph`.

- int ppl_Polyhedron_refine_with_constraint (ppl_Polyhedron_t ph, ppl_const_Constraint_t c)

  Refines `ph` using constraint `c`.

- int ppl_Polyhedron_refine_with_congruence (ppl_Polyhedron_t ph, ppl_const_Congruence_t c)

  Refines `ph` using congruence `c`.

- int ppl_Polyhedron_refine_with_constraints (ppl_Polyhedron_t ph, ppl_const_Constraint_-System_t cs)

  Refines `ph` using the constraints in `cs`.

- int ppl_Polyhedron_refine_with_congruences (ppl_Polyhedron_t ph, ppl_const_Congruence_-System_t cs)

  Refines `ph` using the congruences in `cs`.

- int ppl_Polyhedron_intersection_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

  Intersects `x` with polyhedron `y` and assigns the result to `x`.

- int ppl_Polyhedron_upper_bound_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

  Assigns to `x` an upper bound of `x` and `y`.

- int ppl_Polyhedron_difference_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

  Same as ppl_Polyhedron_poly_difference_assign(x, y).

- int ppl_Polyhedron_simplify_using_context_assign (ppl_Polyhedron_t x, ppl_const_-Polyhedron_t y)

  Assigns to `x` the meet-preserving simplification of `x` with respect to context `y`. Returns a positive integer if `x` and `y` have a nonempty intersection; returns `0` if they are disjoint.

- int ppl_Polyhedron_time_elapse_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

  Assigns to `x` the time-elapse between the polyhedra `x` and `y`.

- int ppl_Polyhedron_topological_closure_assign (ppl_Polyhedron_t ph)

  Assigns to `ph` its topological closure.

- int ppl_Polyhedron_unconstrain_space_dimension (ppl_Polyhedron_t ph, ppl_dimension_type var)

  Modifies `ph` by unconstraining the space dimension `var`.

- int ppl_Polyhedron_unconstrain_space_dimensions (ppl_Polyhedron_t ph, ppl_dimension_type ds[ ], size_t n)

  Modifies `ph` by unconstraining the space dimensions that are specified in the first `n` positions of the array `ds`. The presence of duplicates in `ds` is a waste but an innocuous one.

- int ppl_Polyhedron_affine_image (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_-Linear_Expression_t le, ppl_const_Coefficient_t d)

  Transforms the polyhedron `ph`, assigning an affine expression to the specified variable.

- int ppl_Polyhedron_affine_preimage (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_Linear_Expression_t le, ppl_const_Coefficient_t d)

  Transforms the polyhedron `ph`*, substituting an affine expression to the specified variable.*

- int ppl_Polyhedron_bounded_affine_image (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_Linear_Expression_t lb, ppl_const_Linear_Expression_t ub, ppl_const_Coefficient_t d)

  Assigns to `ph` *the image of* `ph` *with respect to the generalized affine transfer relation* $\frac{\mathrm{lb}}{\mathrm{d}} \leq \mathrm{var}' \leq \frac{\mathrm{ub}}{\mathrm{d}}$.

- int ppl_Polyhedron_bounded_affine_preimage (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_Linear_Expression_t lb, ppl_const_Linear_Expression_t ub, ppl_const_Coefficient_t d)

  Assigns to `ph` *the preimage of* `ph` *with respect to the generalized affine transfer relation* $\frac{\mathrm{lb}}{\mathrm{d}} \leq \mathrm{var}' \leq \frac{\mathrm{ub}}{\mathrm{d}}$.

- int ppl_Polyhedron_generalized_affine_image (ppl_Polyhedron_t ph, ppl_dimension_type var, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_Expression_t le, ppl_const_Coefficient_t d)

  Assigns to `ph` *the image of* `ph` *with respect to the generalized affine transfer relation* $\mathrm{var}' \bowtie \frac{\mathrm{le}}{\mathrm{d}}$*, where* $\bowtie$ *is the relation symbol encoded by* `relsym`.

- int ppl_Polyhedron_generalized_affine_preimage (ppl_Polyhedron_t ph, ppl_dimension_type var, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_Expression_t le, ppl_const_Coefficient_t d)

  Assigns to `ph` *the preimage of* `ph` *with respect to the generalized affine transfer relation* $\mathrm{var}' \bowtie \frac{\mathrm{le}}{\mathrm{d}}$*, where* $\bowtie$ *is the relation symbol encoded by* `relsym`.

- int ppl_Polyhedron_generalized_affine_image_lhs_rhs (ppl_Polyhedron_t ph, ppl_const_Linear_Expression_t lhs, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_Expression_t rhs)

  Assigns to `ph` *the image of* `ph` *with respect to the generalized affine transfer relation* $\mathrm{lhs}' \bowtie \mathrm{rhs}$*, where* $\bowtie$ *is the relation symbol encoded by* `relsym`.

- int ppl_Polyhedron_generalized_affine_preimage_lhs_rhs (ppl_Polyhedron_t ph, ppl_const_Linear_Expression_t lhs, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_Expression_t rhs)

  Assigns to `ph` *the preimage of* `ph` *with respect to the generalized affine transfer relation* $\mathrm{lhs}' \bowtie \mathrm{rhs}$*, where* $\bowtie$ *is the relation symbol encoded by* `relsym`.

Functions that May Modify the Dimension of the Vector Space

- int ppl_Polyhedron_concatenate_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

  Seeing a polyhedron as a set of tuples (its points), assigns to `x` *all the tuples that can be obtained by concatenating, in the order given, a tuple of* `x` *with a tuple of* `y`.

- int ppl_Polyhedron_add_space_dimensions_and_embed (ppl_Polyhedron_t ph, ppl_dimension_type d)

  Adds `d` *new dimensions to the space enclosing the polyhedron* `ph` *and to* `ph` *itself.*

- int ppl_Polyhedron_add_space_dimensions_and_project (ppl_Polyhedron_t ph, ppl_dimension_type d)

  Adds `d` *new dimensions to the space enclosing the polyhedron* `ph`.

- int ppl_Polyhedron_remove_space_dimensions (ppl_Polyhedron_t ph, ppl_dimension_type ds[ ], size_t n)

Removes from the vector space enclosing `ph` *the space dimensions that are specified in first* `n` *positions of the array* `ds`*. The presence of duplicates in* `ds` *is a waste but an innocuous one.*

- int ppl_Polyhedron_remove_higher_space_dimensions (ppl_Polyhedron_t ph, ppl_dimension_type d)

  Removes the higher dimensions from the vector space enclosing `ph` *so that, upon successful return, the new space dimension is* `d`*.*

- int ppl_Polyhedron_map_space_dimensions (ppl_Polyhedron_t ph, ppl_dimension_type maps[ ], size_t n)

  Remaps the dimensions of the vector space according to a partial function. This function is specified by means of the `maps` *array, which has* `n` *entries.*

- int ppl_Polyhedron_expand_space_dimension (ppl_Polyhedron_t ph, ppl_dimension_type d, ppl_dimension_type m)

  Expands the d-th dimension of the vector space enclosing `ph` *to* `m` *new space dimensions.*

- int ppl_Polyhedron_fold_space_dimensions (ppl_Polyhedron_t ph, ppl_dimension_type ds[ ], size_t n, ppl_dimension_type d)

  Modifies `ph` *by folding the space dimensions contained in the first* `n` *positions of the array* `ds` *into dimension* `d`*. The presence of duplicates in* `ds` *is a waste but an innocuous one.*

Input/Output Functions

- int ppl_io_print_Polyhedron (ppl_const_Polyhedron_t x)

  Prints `x` *to* `stdout`*.*

- int ppl_io_fprint_Polyhedron (FILE *stream, ppl_const_Polyhedron_t x)

  Prints `x` *to the given output* `stream`*.*

- int ppl_io_asprint_Polyhedron (char **strp, ppl_const_Polyhedron_t x)

  Prints `x` *to a malloc-allocated string, a pointer to which is returned via* `strp`*.*

- int ppl_Polyhedron_ascii_dump (ppl_const_Polyhedron_t x, FILE *stream)

  Dumps an ascii representation of `x` *on* `stream`*.*

- int ppl_Polyhedron_ascii_load (ppl_Polyhedron_t x, FILE *stream)

  Loads an ascii representation of `x` *from* `stream`*.*

Ad Hoc Functions for (C or NNC) Polyhedra

The functions listed here below, being specific of the polyhedron domains, do not have a correspondence in other semantic geometric descriptions.

- int ppl_new_C_Polyhedron_from_Generator_System (ppl_Polyhedron_t *pph, ppl_const_Generator_System_t gs)

  Builds a new C polyhedron from the system of generators `gs` *and writes a handle for the newly created polyhedron at address* `pph`*.*

- int ppl_new_C_Polyhedron_recycle_Generator_System (ppl_Polyhedron_t *pph, ppl_Generator_System_t gs)

  Builds a new C polyhedron recycling the system of generators `gs` *and writes a handle for the newly created polyhedron at address* `pph`*.*

- int ppl_new_NNC_Polyhedron_from_Generator_System (ppl_Polyhedron_t *pph, ppl_const_Generator_System_t gs)

  Builds a new NNC polyhedron from the system of generators `gs` *and writes a handle for the newly created polyhedron at address* `pph`.

- int ppl_new_NNC_Polyhedron_recycle_Generator_System (ppl_Polyhedron_t *pph, ppl_Generator_System_t gs)

  Builds a new NNC polyhedron recycling the system of generators `gs` *and writes a handle for the newly created polyhedron at address* `pph`.

- int ppl_Polyhedron_get_generators (ppl_const_Polyhedron_t ph, ppl_const_Generator_System_t *pgs)

  Writes a const handle to the generator system defining the polyhedron `ph` *at address* `pgs`.

- int ppl_Polyhedron_get_minimized_generators (ppl_const_Polyhedron_t ph, ppl_const_Generator_System_t *pgs)

  Writes a const handle to the minimized generator system defining the polyhedron `ph` *at address* `pgs`.

- int ppl_Polyhedron_add_generator (ppl_Polyhedron_t ph, ppl_const_Generator_t g)

  Adds a copy of the generator `g` *to the system of generators of* `ph`.

- int ppl_Polyhedron_add_generators (ppl_Polyhedron_t ph, ppl_const_Generator_System_t gs)

  Adds a copy of the system of generators `gs` *to the system of generators of* `ph`.

- int ppl_Polyhedron_add_recycled_generators (ppl_Polyhedron_t ph, ppl_Generator_System_t gs)

  Adds the system of generators `gs` *to the system of generators of* `ph`.

- int ppl_Polyhedron_poly_hull_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

  Assigns to `x` *the poly-hull of* `x` *and* `y`.

- int ppl_Polyhedron_poly_difference_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

  Assigns to `x` *the poly-difference of* `x` *and* `y`.

- int wrap_assign (ppl_Polyhedron_t ph, ppl_dimension_type ds[ ], size_t n, ppl_enum_Bounded_Integer_Type_Width w, ppl_enum_Bounded_Integer_Type_Representation r, ppl_enum_Bounded_Integer_Type_Overflow o, const ppl_const_Constraint_System_t *pcs, unsigned complexity_threshold, int wrap_individually)

  Assigns to `ph` *the polyhedron obtained from* `ph` *by "wrapping" the vector space defined by the first* `n` *space dimensions in* `ds[]`.

- int ppl_Polyhedron_BHRZ03_widening_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, unsigned *tp)

  If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the BHRZ03-widening of* `x` *and* `y`*. If* `tp` *is not the null pointer, the widening with tokens delay technique is applied with* `*tp` *available tokens.*

- int ppl_Polyhedron_H79_widening_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, unsigned *tp)

  If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the H79-widening of* `x` *and* `y`*. If* `tp` *is not the null pointer, the widening with tokens delay technique is applied with* `*tp` *available tokens.*

- int ppl_Polyhedron_BHRZ03_widening_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

  If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the BHRZ03-widening of* `x` *and* `y`*.*

- int ppl_Polyhedron_H79_widening_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

  If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the H79-widening of* `x` *and* `y`*.*

- int ppl_Polyhedron_limited_BHRZ03_extrapolation_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)

  If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the BHRZ03-widening of* `x` *and* `y` *intersected with the constraints in* `cs` *that are satisfied by all the points of* `x`*. If* `tp` *is not the null pointer, the widening with tokens delay technique is applied with* `*tp` *available tokens.*

- int ppl_Polyhedron_limited_H79_extrapolation_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)

  If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the H79-widening of* `x` *and* `y` *intersected with the constraints in* `cs` *that are satisfied by all the points of* `x`*. If* `tp` *is not the null pointer, the widening with tokens delay technique is applied with* `*tp` *available tokens.*

- int ppl_Polyhedron_limited_BHRZ03_extrapolation_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs)

  If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the BHRZ03-widening of* `x` *and* `y` *intersected with the constraints in* `cs` *that are satisfied by all the points of* `x`*.*

- int ppl_Polyhedron_limited_H79_extrapolation_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs)

  If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the H79-widening of* `x` *and* `y` *intersected with the constraints in* `cs` *that are satisfied by all the points of* `x`*.*

- int ppl_Polyhedron_bounded_BHRZ03_extrapolation_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)

  If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the BHRZ03-widening of* `x` *and* `y` *intersected with the constraints in* `cs` *that are satisfied by all the points of* `x`*, further intersected with all the constraints of the form* $\pm v \leq r$ *and* $\pm v < r$*, with* $r \in \mathbb{Q}$*, that are satisfied by all the points of* `x`*. If* `tp` *is not the null pointer, the widening with tokens delay technique is applied with* `*tp` *available tokens.*

- int ppl_Polyhedron_bounded_H79_extrapolation_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)

  If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the H79-widening of* `x` *and* `y` *intersected with the constraints in* `cs` *that are satisfied by all the points of* `x`*, further intersected with all the constraints of the form* $\pm v \leq r$ *and* $\pm v < r$*, with* $r \in \mathbb{Q}$*, that are satisfied by all the points of* `x`*. If* `tp` *is not the null pointer, the widening with tokens delay technique is applied with* `*tp` *available tokens.*

- int ppl_Polyhedron_bounded_BHRZ03_extrapolation_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs)

  If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the BHRZ03-widening of* `x` *and* `y` *intersected with the constraints in* `cs` *that are satisfied by all the points of* `x`*, further intersected with all the constraints of the form* $\pm v \leq r$ *and* $\pm v < r$*, with* $r \in \mathbb{Q}$*, that are satisfied by all the points of* `x`*.*

- int ppl_Polyhedron_bounded_H79_extrapolation_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs)

If the polyhedron `y` *is contained in (or equal to) the polyhedron* `x`*, assigns to* `x` *the H79-widening of* `x` *and* `y` *intersected with the constraints in* `cs` *that are satisfied by all the points of* `x`*, further intersected with all the constraints of the form* $\pm v \leq r$ *and* $\pm v < r$*, with* $r \in \mathbb{Q}$*, that are satisfied by all the points of* `x`*.*

7.25.1 Detailed Description

Types and functions for the domains of C and NNC convex polyhedra. The types and functions for convex polyhedra provide a single interface for accessing both topologically closed (C) and not necessarily closed (NNC) convex polyhedra. The distinction between C and NNC polyhedra need only be explicitly stated when *creating* or *assigning* a polyhedron object, by means of one of the functions `ppl_new_*` and `ppl_assign_*`.

Having a single datatype does not mean that C and NNC polyhedra can be freely interchanged: as specified in the main manual, most library functions require their arguments to be topologically and/or space-dimension compatible.

7.25.2 Friends And Related Function Documentation

7.25.2.1 int ppl_new_C_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t * *pph*, ppl_const_Polyhedron_t *ph*, int *complexity*) `[related]`

Builds a C polyhedron that is a copy of `ph`; writes a handle for the newly created polyhedron at address `pph`.

Note

The complexity argument is ignored.

7.25.2.2 int ppl_new_C_Polyhedron_from_Constraint_System (ppl_Polyhedron_t * *pph*, ppl_const_Constraint_System_t *cs*) `[related]`

Builds a new C polyhedron from the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `cs`.

7.25.2.3 int ppl_new_C_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t * *pph*, ppl_Constraint_System_t *cs*) `[related]`

Builds a new C polyhedron recycling the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `cs`.

Warning

This function modifies the constraint system referenced by `cs`: upon return, no assumption can be made on its value.

7.25.2.4 int ppl_new_C_Polyhedron_from_Congruence_System (ppl_Polyhedron_t * *pph*, ppl_const_Congruence_System_t *cs*) `[related]`

Builds a new C polyhedron from the system of congruences `cs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `cs`.

7.25.2.5 int ppl_new_C_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t * *pph*, ppl_Congruence_System_t *cs*) `[related]`

Builds a new C polyhedron recycling the system of congruences `cs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `cs`.

Warning

This function modifies the congruence system referenced by `cs`: upon return, no assumption can be made on its value.

7.25.2.6 int ppl_new_NNC_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t * *pph*, ppl_const_Polyhedron_t *ph*, int *complexity*) `[related]`

Builds an NNC polyhedron that is a copy of `ph`; writes a handle for the newly created polyhedron at address `pph`.

Note

The complexity argument is ignored.

7.25.2.7 int ppl_new_NNC_Polyhedron_from_Constraint_System (ppl_Polyhedron_t * *pph*, ppl_const_Constraint_System_t *cs*) `[related]`

Builds a new NNC polyhedron from the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `cs`.

7.25.2.8 int ppl_new_NNC_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t * *pph*, ppl_Constraint_System_t *cs*) [related]

Builds a new NNC polyhedron recycling the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `cs`.

Warning

This function modifies the constraint system referenced by `cs`: upon return, no assumption can be made on its value.

7.25.2.9 int ppl_new_NNC_Polyhedron_from_Congruence_System (ppl_Polyhedron_t * *pph*, ppl_const_Congruence_System_t *cs*) [related]

Builds a new NNC polyhedron from the system of congruences `cs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `cs`.

7.25.2.10 int ppl_new_NNC_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t * *pph*, ppl_Congruence_System_t *cs*) [related]

Builds a new NNC polyhedron recycling the system of congruences `cs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `cs`.

Warning

This function modifies the congruence system referenced by `cs`: upon return, no assumption can be made on its value.

7.25.2.11 int ppl_new_C_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t * *pph*, ppl_const_Polyhedron_t *ph*, int *complexity*) [related]

Builds a C polyhedron that approximates NNC_Polyhedron `ph`, using an algorithm whose complexity does not exceed `complexity`; writes a handle for the newly created polyhedron at address `pph`.

Note

The complexity argument, which can take values `PPL_COMPLEXITY_CLASS_POLYNOMIAL`, `PPL_COMPLEXITY_CLASS_SIMPLEX` and `PPL_COMPLEXITY_CLASS_ANY`, is ignored since the exact constructor has polynomial complexity.

7.25.2.12 int ppl_new_NNC_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t * *pph*, ppl_const_Polyhedron_t *ph*, int *complexity*) [related]

Builds an NNC polyhedron that approximates C_Polyhedron `ph`, using an algorithm whose complexity does not exceed `complexity`; writes a handle for the newly created polyhedron at address `pph`.

Note

The complexity argument, which can take values `PPL_COMPLEXITY_CLASS_POLYNOMIAL`, `PPL_COMPLEXITY_CLASS_SIMPLEX` and `PPL_COMPLEXITY_CLASS_ANY`, is ignored since the exact constructor has polynomial complexity.

7.25.2.13 int ppl_Polyhedron_relation_with_Constraint (ppl_const_Polyhedron_t *ph*, ppl_const_Constraint_t *c*) [related]

Checks the relation between the polyhedron `ph` and the constraint `c`.

If successful, returns a non-negative integer that is obtained as the bitwise or of the bits (chosen among PPL_POLY_CON_RELATION_IS_DISJOINT PPL_POLY_CON_RELATION_STRICTLY_-INTERSECTS, PPL_POLY_CON_RELATION_IS_INCLUDED, and PPL_POLY_CON_RELATION_-SATURATES) that describe the relation between `ph` and `c`.

7.25.2.14 int ppl_Polyhedron_relation_with_Generator (ppl_const_Polyhedron_t *ph*, ppl_const_Generator_t *g*) [related]

Checks the relation between the polyhedron `ph` and the generator `g`.

If successful, returns a non-negative integer that is obtained as the bitwise or of the bits (only PPL_POLY_-GEN_RELATION_SUBSUMES, at present) that describe the relation between `ph` and `g`.

7.25.2.15 int ppl_Polyhedron_maximize_with_point (ppl_const_Polyhedron_t *ph*, ppl_const_Linear_Expression_t *le*, ppl_Coefficient_t *sup_n*, ppl_Coefficient_t *sup_d*, int * *pmaximum*, ppl_Generator_t *point*) [related]

Returns a positive integer if `ph` is not empty and `le` is bounded from above in `ph`, in which case the supremum value and a point where `le` reaches it are computed.

Parameters

ph The polyhedron constraining `le`;

le The linear expression to be maximized subject to `ph`;

sup_n Will be assigned the numerator of the supremum value;

sup_d Will be assigned the denominator of the supremum value;

pmaximum Will store 1 in this location if the supremum is also the maximum, will store 0 otherwise;

point Will be assigned the point or closure point where `le` reaches the extremum value.

If `ph` is empty or `le` is not bounded from above, 0 will be returned and `sup_n`, `sup_d`, `*pmaximum` and `point` will be left untouched.

7.25.2.16 int ppl_Polyhedron_minimize_with_point (ppl_const_Polyhedron_t *ph*, ppl_const_Linear_Expression_t *le*, ppl_Coefficient_t *inf_n*, ppl_Coefficient_t *inf_d*, int * *pminimum*, ppl_Generator_t *point*) `[related]`

Returns a positive integer if `ph` is not empty and `le` is bounded from below in `ph`, in which case the infimum value and a point where `le` reaches it are computed.

Parameters

ph The polyhedron constraining `le`;

le The linear expression to be minimized subject to `ph`;

inf_n Will be assigned the numerator of the infimum value;

inf_d Will be assigned the denominator of the infimum value;

pminimum Will store 1 in this location if the infimum is also the minimum, will store 0 otherwise;

point Will be assigned the point or closure point where `le` reaches the extremum value.

If `ph` is empty or `le` is not bounded from below, 0 will be returned and `sup_n`, `sup_d`, `*pmaximum` and `point` will be left untouched.

7.25.2.17 int ppl_Polyhedron_equals_Polyhedron (ppl_const_Polyhedron_t *x*, ppl_const_Polyhedron_t *y*) `[related]`

Returns a positive integer if `x` and `y` are the same polyhedron; returns 0 if they are different.

Note that `x` and `y` may be topology- and/or dimension-incompatible polyhedra: in those cases, the value 0 is returned.

7.25.2.18 int ppl_Polyhedron_add_recycled_constraints (ppl_Polyhedron_t *ph*, ppl_Constraint_System_t *cs*) `[related]`

Adds the system of constraints `cs` to the system of constraints of `ph`.

Warning

This function modifies the constraint system referenced by `cs`: upon return, no assumption can be made on its value.

7.25.2.19 int ppl_Polyhedron_add_recycled_congruences (ppl_Polyhedron_t *ph*, ppl_Congruence_System_t *cs*) `[related]`

Adds the system of congruences `cs` to the polyhedron `ph`.

Warning

This function modifies the congruence system referenced by `cs`: upon return, no assumption can be made on its value.

7.25.2.20 int ppl_Polyhedron_upper_bound_assign (ppl_Polyhedron_t *x*, ppl_const_Polyhedron_t *y*) [related]

Assigns to `x` an upper bound of `x` and `y`.

For the domain of polyhedra, this is the same as `ppl_Polyhedron_poly_hull_assign(x, y)`.

7.25.2.21 int ppl_Polyhedron_affine_image (ppl_Polyhedron_t *ph*, ppl_dimension_type *var*, ppl_const_Linear_Expression_t *le*, ppl_const_Coefficient_t *d*) [related]

Transforms the polyhedron `ph`, assigning an affine expression to the specified variable.

Parameters

ph The polyhedron that is transformed;

var The variable to which the affine expression is assigned;

le The numerator of the affine expression;

d The denominator of the affine expression.

7.25.2.22 int ppl_Polyhedron_affine_preimage (ppl_Polyhedron_t *ph*, ppl_dimension_type *var*, ppl_const_Linear_Expression_t *le*, ppl_const_Coefficient_t *d*) [related]

Transforms the polyhedron `ph`, substituting an affine expression to the specified variable.

Parameters

ph The polyhedron that is transformed;

var The variable to which the affine expression is substituted;

le The numerator of the affine expression;

d The denominator of the affine expression.

7.25.2.23 int ppl_Polyhedron_bounded_affine_image (ppl_Polyhedron_t *ph*, ppl_dimension_type *var*, ppl_const_Linear_Expression_t *lb*, ppl_const_Linear_Expression_t *ub*, ppl_const_Coefficient_t *d*) [related]

Assigns to `ph` the image of `ph` with respect to the *generalized affine transfer relation* $\frac{\mathrm{lb}}{\mathrm{d}} \leq \mathrm{var}' \leq \frac{\mathrm{ub}}{\mathrm{d}}$.

Parameters

ph The polyhedron that is transformed;

var The variable bounded by the generalized affine transfer relation;

lb The numerator of the lower bounding affine expression;

ub The numerator of the upper bounding affine expression;

d The (common) denominator of the lower and upper bounding affine expressions.

7.25.2.24 int ppl_Polyhedron_bounded_affine_preimage (ppl_Polyhedron_t *ph*, ppl_dimension_type *var*, ppl_const_Linear_Expression_t *lb*, ppl_const_Linear_Expression_t *ub*, ppl_const_Coefficient_t *d*) `[related]`

Assigns to `ph` the preimage of `ph` with respect to the *generalized affine transfer relation* $\frac{\mathrm{lb}}{\mathrm{d}} \leq \mathrm{var}' \leq \frac{\mathrm{ub}}{\mathrm{d}}$.

Parameters

ph The polyhedron that is transformed;

var The variable bounded by the generalized affine transfer relation;

lb The numerator of the lower bounding affine expression;

ub The numerator of the upper bounding affine expression;

d The (common) denominator of the lower and upper bounding affine expressions.

7.25.2.25 int ppl_Polyhedron_generalized_affine_image (ppl_Polyhedron_t *ph*, ppl_dimension_type *var*, enum ppl_enum_Constraint_Type *relsym*, ppl_const_Linear_Expression_t *le*, ppl_const_Coefficient_t *d*) `[related]`

Assigns to `ph` the image of `ph` with respect to the *generalized affine transfer relation* $\mathrm{var}' \bowtie \frac{\mathrm{le}}{\mathrm{d}}$, where $\bowtie$ is the relation symbol encoded by `relsym`.

Parameters

ph The polyhedron that is transformed;

var The left hand side variable of the generalized affine transfer relation;

relsym The relation symbol;

le The numerator of the right hand side affine expression;

d The denominator of the right hand side affine expression.

7.25.2.26 int ppl_Polyhedron_generalized_affine_preimage (ppl_Polyhedron_t *ph*, ppl_dimension_type *var*, enum ppl_enum_Constraint_Type *relsym*, ppl_const_Linear_Expression_t *le*, ppl_const_Coefficient_t *d*) `[related]`

Assigns to `ph` the preimage of `ph` with respect to the *generalized affine transfer relation* $\mathrm{var}' \bowtie \frac{\mathrm{le}}{\mathrm{d}}$, where $\bowtie$ is the relation symbol encoded by `relsym`.

Parameters

ph The polyhedron that is transformed;

var The left hand side variable of the generalized affine transfer relation;

relsym The relation symbol;

le The numerator of the right hand side affine expression;

d The denominator of the right hand side affine expression.

7.25.2.27 int ppl_Polyhedron_generalized_affine_image_lhs_rhs (ppl_Polyhedron_t *ph*, ppl_const_Linear_Expression_t *lhs*, enum ppl_enum_Constraint_Type *relsym*, ppl_const_Linear_Expression_t *rhs*) `[related]`

Assigns to `ph` the image of `ph` with respect to the *generalized affine transfer relation* $\mathrm{lhs}' \bowtie \mathrm{rhs}$, where $\bowtie$ is the relation symbol encoded by `relsym`.

Parameters

ph The polyhedron that is transformed;

lhs The left hand side affine expression;

relsym The relation symbol;

rhs The right hand side affine expression.

7.25.2.28 int ppl_Polyhedron_generalized_affine_preimage_lhs_rhs (ppl_Polyhedron_t *ph*, ppl_const_Linear_Expression_t *lhs*, enum ppl_enum_Constraint_Type *relsym*, ppl_const_Linear_Expression_t *rhs*) `[related]`

Assigns to `ph` the preimage of `ph` with respect to the *generalized affine transfer relation* $\mathrm{lhs}' \bowtie \mathrm{rhs}$, where $\bowtie$ is the relation symbol encoded by `relsym`.

Parameters

ph The polyhedron that is transformed;

lhs The left hand side affine expression;

relsym The relation symbol;

rhs The right hand side affine expression.

7.25.2.29 int ppl_Polyhedron_map_space_dimensions (ppl_Polyhedron_t *ph*, ppl_dimension_type *maps*[ ], size_t *n*) `[related]`

Remaps the dimensions of the vector space according to a *partial function*. This function is specified by means of the `maps` array, which has `n` entries.

The partial function is defined on dimension `i` if `i < n` and `maps[i] != ppl_not_a_dimension`; otherwise it is undefined on dimension `i`. If the function is defined on dimension `i`, then dimension `i` is mapped onto dimension `maps[i]`.

The result is undefined if `maps` does not encode a partial function with the properties described in the *specification of the mapping operator*.

7.25.2.30 int ppl_new_C_Polyhedron_from_Generator_System (ppl_Polyhedron_t * *pph*, ppl_const_Generator_System_t *gs*) [related]

Builds a new C polyhedron from the system of generators `gs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `gs`.

7.25.2.31 int ppl_new_C_Polyhedron_recycle_Generator_System (ppl_Polyhedron_t * *pph*, ppl_Generator_System_t *gs*) [related]

Builds a new C polyhedron recycling the system of generators `gs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `gs`.

Warning

This function modifies the generator system referenced by `gs`: upon return, no assumption can be made on its value.

7.25.2.32 int ppl_new_NNC_Polyhedron_from_Generator_System (ppl_Polyhedron_t * *pph*, ppl_const_Generator_System_t *gs*) [related]

Builds a new NNC polyhedron from the system of generators `gs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `gs`.

7.25.2.33 int ppl_new_NNC_Polyhedron_recycle_Generator_System (ppl_Polyhedron_t * *pph*, ppl_Generator_System_t *gs*) [related]

Builds a new NNC polyhedron recycling the system of generators `gs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `gs`.

Warning

This function modifies the generator system referenced by `gs`: upon return, no assumption can be made on its value.

7.25.2.34 int ppl_Polyhedron_add_recycled_generators (ppl_Polyhedron_t *ph*, ppl_Generator_System_t *gs*) [related]

Adds the system of generators `gs` to the system of generators of `ph`.

Warning

This function modifies the generator system referenced by `gs`: upon return, no assumption can be made on its value.

7.25.2.35 int wrap_assign (ppl_Polyhedron_t *ph*, ppl_dimension_type *ds*[ ], size_t *n*, ppl_enum_Bounded_Integer_Type_Width *w*, ppl_enum_Bounded_Integer_Type_Representation *r*, ppl_enum_Bounded_Integer_Type_Overflow *o*, const ppl_const_Constraint_System_t * *pcs*, unsigned *complexity_threshold*, int *wrap_individually*) `[related]`

Assigns to `ph` the polyhedron obtained from `ph` by "wrapping" the vector space defined by the first `n` space dimensions in `ds`[].

Parameters

ph The polyhedron that is transformed;

ds[ ] Specifies the space dimensions to be wrapped.

n The first `n` space dimensions in the array `ds`[] will be wrapped.

w The width of the bounded integer type corresponding to all the dimensions to be wrapped.

r The representation of the bounded integer type corresponding to all the dimensions to be wrapped.

o The overflow behavior of the bounded integer type corresponding to all the dimensions to be wrapped.

pcs Possibly null pointer to a constraint system whose space dimensions are the first `n` dimensions in `ds`[]. If `*pcs` depends on variables not in `vars`, the behavior is undefined. When non-null, the constraint system is assumed to represent the conditional or looping construct guard with respect to which wrapping is performed. Since wrapping requires the computation of upper bounds and due to non-distributivity of constraint refinement over upper bounds, passing a constraint system in this way can be more precise than refining the result of the wrapping operation with the constraints in `cs`.

complexity_threshold A precision parameter where higher values result in possibly improved precision.

wrap_individually Non-zero if the dimensions should be wrapped individually (something that results in much greater efficiency to the detriment of precision).

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