The Parma Polyhedra Library OCaml Language Interface User's Manual* (version 0.11.2)

Roberto Bagnara†
Patricia M. Hill‡
Enea Zaffanella§

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†bagnara@cs.unipr.it, Department of Mathematics, University of Parma, Italy.
‡hill@comp.leeds.ac.uk, School of Computing, University of Leeds, U.K.
§zaffanella@cs.unipr.it, Department of Mathematics, University of Parma, Italy.

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http://www.cs.unipr.it/ppl/

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1 OCaml Language Interface

The Parma Polyhedra Library comes equipped with an interface for the OCaml language.

The main features of the library are described in Section OCaml Interface Features. Section OCamldoc Documentation lists all the functions available to the default generated domains in the OCaml interface. Section Compilation and Installation explains how the OCaml interface is compiled and installed.

In the sequel, `prefix` is the prefix under which you have installed the library (typically `/usr` or `/usr/local`).

OCaml Interface Features

The OCaml interface provides access to the numerical abstractions (convex polyhedra, BD shapes, octagonal shapes, etc.) implemented by the PPL library. A general introduction to the numerical abstractions, their representation in the PPL and the operations provided by the PPL is given in the main *PPL user manual*. Here we just describe those aspects that are specific to the OCaml interface.

Overview

First, here is a list of notes with general information and advice on the use of the OCaml interface.

- The numerical abstract domains available to the OCaml user consist of the *simple* domains, *powersets* of a simple domain and *products* of simple domains.
  - The simple domains are:
    - convex polyhedra, which consist of C_Polyhedron and NNC_Polyhedron;
    - weakly relational, which consist of BD_Shape_N and Octagonal_Shape_N where N is one of the numeric types short, signed_char, int, long, long_long, mpz_class, mpq_class;
    - boxes which consist of Int8_Box, Int16_Box, Int32_Box, Int64_Box, Uint8_Box, Uint16_Box, Uint32_Box, Uint64_Box, Double_Box, Long_Double_Box, Z_Box, Rational_Box, Float_Box; and
    - the Grid domain.
  - The powerset domains are Pointset_Powerset_S where S is a simple domain.
  - The product domains consist of Direct_Product_S_T, Smash_Product_S_T and Constraints_-Product_S_T where S and T are simple domains.
- In the following, any of the above numerical abstract domains is called a PPL *domain* and any element of a PPL domain is called a *PPL object*.
- The OCaml interface files are all installed in the directory `prefix/lib/ppl`. Since this includes shared and dynamically loaded libraries, you must make your dynamic linker/loader aware of this fact. If you use a GNU/Linux system, try the commands `man ld.so` and `man ldconfig` for more information.
- A PPL object such as a polyhedron can only be accessed by means of a OCaml term called a *handle*. Note, however, that the data structure of a handle, is implementation-dependent, system-dependent and version-dependent, and, for this reason, deliberately left unspecified. What we do guarantee is that the handle requires very little memory.
- An OCaml program can obtain a valid handle for a PPL object by using functions such as

  ```
  ppl_new_C_Polyhedron_from_space_dimension,
  ppl_new_C_Polyhedron_from_C_Polyhedron,
  ppl_new_C_Polyhedron_from_constraints,
  ppl_new_C_Polyhedron_from_generators.
  ```

  These functions will return a new handle for referencing a PPL polyhedron.
- For a PPL object with space dimension `k`, the identifiers used for the PPL variables must lie between 0 and $k-1$ and correspond to the indices of the associated Cartesian axes. For example, when using the functions that combine PPL polyhedra or add constraints or generators to a representation of a PPL polyhedron, the polyhedra referenced and any constraints or generators in the call should follow all the (space) dimension-compatibility rules stated in Section *Representations of Convex Polyhedra* of the main PPL user manual.

- As explained above, a polyhedron has a fixed topology C or NNC, that is determined at the time of its initialization. All subsequent operations on the polyhedron must respect all the topological compatibility rules stated in Section *Representations of Convex Polyhedra* of the main PPL user manual.
- Any application using the PPL should make sure that only the intended version(s) of the library are ever used. Functions

```
ppl_version_major,
ppl_version_minor,
ppl_version_revision,
ppl_version_beta,
ppl_version,
ppl_banner.
```

  allow run-time checking of information about the version being used.

Function Descriptions

Below is a short description of many of the interface functions. For full definitions of terminology used here, see the main PPL user manual.

Domain Independent Functions

First we describe some domain independent functions included with all instantiations of the OCaml interfaces.

`ppl_version_major`

Returns the major number of the PPL version.

`ppl_version_minor`

Returns the minor number of the PPL version.

`ppl_version_revision`

Returns the revision number of the PPL version.

`ppl_version_beta`

Returns the beta number of the PPL version.

`ppl_version`

Returns the PPL version.

ppl_banner

Returns information about the PPL version, the licensing, the lack of any warranty whatsoever, the C++ compiler used to build the library, where to report bugs and where to look for further information.

ppl_max_space_dimension

Returns the maximum space dimension the C++ interface can handle.

ppl_Coefficient_bits

Returns the number of bits used in the C++ interface for PPL coefficients; 0 if unbounded.

ppl_Coefficient_is_bounded

Returns true if and only if the coefficients in the C++ interface are bounded.

ppl_Coefficient_max

If the coefficients are bounded, returns the maximum coefficient the C++ interface can handle.

ppl_Coefficient_min

If the coefficients are bounded, returns the minimum coefficient the C++ interface can handle.

ppl_io_wrap_string source_string indent_depth preferred_first_line_length preferred_line_length

Utility function for the wrapping of lines of text. The function wraps the lines of text stored in its first string argument according to the next three integer arguments, which are interpreted as the indentation depth, the preferred length for the first line and the preferred length for all the other lines, respecively; it returns a string containing the wrapped text.

ppl_set_timeout hsecs

Computations taking exponential time will be interrupted some time after `hsecs` hundreths of seconds after that call. If the computation is interrupted that way, a timeout exception will be thrown. An exception is immediately thrown if `hsecs` is not strictly greater than zero, or if the PPL Watchdog library is not enabled.

ppl_reset_timeout

Resets the timeout time so that the computation is not interrupted. An exception is thrown if the PPL Watchdog library is not enabled.

ppl_set_deterministic_timeout weight

Computations taking exponential time will be interrupted some time after reaching the `weight` complexity threshold. If the computation is interrupted that way, a timeout exception will be thrown. An exception is immediately thrown if `hsecs` is not strictly greater than zero, or if the PPL Watchdog library is not enabled. *NOTE:* This "timeout" checking functionality is said to be *deterministic* because it is not based on actual elapsed time. Its behavior will only depend on (some of the) computations performed in the PPL library and it will be otherwise independent from the computation environment (CPU, operating system, compiler, etc.). The weight mechanism is under alpha testing: client applications should be ready to reconsider the tuning of these weight thresholds when upgrading to newer version of the PPL.

ppl_reset_deterministic_timeout

Resets the timeout time so that the computation is not interrupted. An exception is thrown if the PPL Watchdog library is not enabled.

ppl_set_rounding_for_PPL

Sets the FPU rounding mode so that the PPL abstractions based on floating point numbers work correctly. This is performed automatically at initialization-time. Calling this function is needed only if `restore_pre_PPL_rounding` has previously been called.

ppl_restore_pre_PPL_rounding

Sets the FPU rounding mode as it was before initialization of the PPL. After calling this function it is absolutely necessary to call `set_rounding_for_PPL` before using any PPL abstractions based on floating point numbers. This is performed automatically at finalization-time.

ppl_irrational_precision

Returns the precision parameter for irrational calculations.

ppl_set_irrational_precision

Sets the precision parameter `p` for irrational calculations. In the following irrational calculations returning an unbounded rational (e.g., when computing a square root), the lesser between numerator and denominator will be limited to `2**p`.

MIP Functions

Here we describe some functions available for PPL objects defining mixed integer (linear) programming problems.

ppl_new_MIP_Problem_from_space_dimension dimension

Return a handle to an MIP Problem MIP with the feasible region the vector space of dimension `dimension`, objective function 0 and optimization mode `max`.

ppl_new_MIP_Problem dimension constraint_system lin_expr optimization_mode

Return a handle to an MIP Problem MIP having space dimension `dimension`, a feasible region represented by `constraint_system`, objective function `lin_expr` and optimization mode `optimization_mode`.

ppl_MIP_Problem_get_control_parameter handle param_name

Returns the value of the control parameter named `param_name`.

ppl_MIP_Problem_set_control_parameter handle param_value

Sets control parameter value `param_value`.

ppl_MIP_Problem_swap handle_1 handle_2

Swaps the MIP Problem referenced by `handle_1` with the one referenced by `handle_2`.

ppl_MIP_Problem_space_dimension handle

Returns the dimension of the vector space in which the MIP Problem referenced by `handle` is embedded.

ppl_MIP_Problem_integer_space_dimensions handle

Returns a list of variables representing representing the integer space dimensions of the MIP Problem referenced by `handle`.

ppl_MIP_Problem_constraints handle

Returns a list of the constraints in the constraints system representing the feasible region for the MIP Problem referenced by `handle`.

ppl_MIP_Problem_objective_function handle

Returns the objective function for the MIP Problem referenced by `handle`.

ppl_MIP_Problem_optimization_mode handle

Returns the optimization mode for the MIP Problem referenced by `handle`.

ppl_MIP_Problem_clear handle

Resets the MIP problem referenced by `handle` to be the trivial problem with the feasible region the 0-dimensional universe, objective function 0 and optimization mode `Maximization`.

ppl_MIP_Problem_add_space_dimensions_and_embed handle dimension

Embeds the MIP problem referenced by `handle` in a space that is enlarged by `dimension` dimensions,

ppl_MIP_Problem_add_to_integer_space_dimensions handle vars_list

Updates the MIP Problem referenced by `handle` so that the variables in `vars_list` are added to the set of integer space dimensions.

ppl_MIP_Problem_add_constraint handle constraint

Updates the MIP Problem referenced by `handle` so that the feasible region is represented by the original constraint system together with the constraint `constraint`.

ppl_MIP_Problem_add_constraints handle constraint_system

Updates the MIP Problem referenced by `handle` so that the feasible region is represented by the original constraint system together with all the constraints in `constraint_system`.

ppl_MIP_Problem_set_objective_function handle lin_expr

Updates the MIP Problem referenced by `handle` so that the objective function is changed to `lin_expr`.

ppl_MIP_Problem_set_optimization_mode handle optimization_mode

Updates the MIP Problem referenced by `handle` so that the optimization mode is changed to `optimization_mode`.

ppl_MIP_Problem_is_satisfiable handle

Returns true if the MIP Problem referenced by `handle` is satisfiable and false otherwise.

ppl_MIP_Problem_solve handle

Solves the MIP problem referenced by `handle` and returns 0, if the MIP problem is not satisfiable; 1, if the MIP problem is satisfiable but there is no finite bound to the value of the objective function; 2, if the MIP problem admits an optimal solution.

ppl_MIP_Problem_feasible_point handle

Returns a feasible point for the MIP problem referenced by `handle`.

ppl_MIP_Problem_optimizing_point handle

Returns an optimizing point for the MIP problem referenced by `handle`.

ppl_MIP_Problem_optimal_value handle

Returns a pair of numbers, the first being the numerator and the second the denominator, for the optimal value for the MIP problem referenced by `handle`.

ppl_MIP_Problem_evaluate_objective_function handle generator

Evaluates the objective function of the MIP problem referenced by `handle` at point `generator`. Returns a pair of numbers, the first being the numerator and the second the denominator, for the objective function value for the MIP problem referenced by `handle`.

ppl_MIP_Problem_OK handle

Returns true if the MIP Problem referenced by `handle` is well formed, i.e., if it satisfies all its implementation invariants and false, otherwise. Useful for debugging purposes.

ppl_MIP_Problem_ascii_dump handle

Returns a string containing an ASCII dump of the internal representation of the MIP_Problem referenced by `handle`. Useful for debugging purposes.

PIP Functions

Here we describe some functions available for PPL objects defining parametric integer programming problems.

ppl_new_PIP_Problem_from_space_dimension dimension

Return a handle to a PIP Problem PIP with the feasible region the vector space of dimension `dimension`, empty constraint_system and empty set of parametric variables.

ppl_new_PIP_Problem dimension constraint_system vars_list

Return a handle to a PIP Problem PIP having space dimension `dimension`, a feasible region represented by `constraint_system` and parametric variables represented by `vars_list`.

ppl_PIP_Problem_get_control_parameter handle param_name

Returns the value of the control parameter named `param_name`.

ppl_PIP_Problem_set_control_parameter handle param_value

Sets control parameter value `param_value`.

ppl_PIP_Problem_swap handle_1 handle_2

Swaps the PIP Problem referenced by `handle_1` with the one referenced by `handle_2`.

ppl_PIP_Problem_space_dimension handle

Returns the dimension of the vector space in which the PIP Problem referenced by `handle` is embedded.

ppl_PIP_Problem_parameter_space_dimensions handle

Returns a list of variables representing representing the parameter space dimensions of the PIP Problem referenced by `handle`.

ppl_PIP_Problem_constraints handle

Returns a list of the constraints in the constraints system representing the feasible region for the PIP Problem referenced by `handle`.

ppl_PIP_Problem_clear handle

Resets the PIP problem referenced by `handle` to be the trivial problem with space dimension 0.

ppl_PIP_Problem_add_space_dimensions_and_embed handle dimension_0 dimension_1

Embeds the PIP problem referenced by `handle` in a space that is enlarged by `dimension_0` non-parameter dimensions and `dimension_1` parameter dimensions,

ppl_PIP_Problem_add_to_parameter_space_dimensions handle vars_list

Sets the space dimensions whose indexes are in `vars_list` to be parameter space dimensions.

ppl_PIP_Problem_add_constraint handle constraint

Updates the PIP Problem referenced by `handle` so that the feasible region is represented by the original constraint system together with the constraint `constraint`.

ppl_PIP_Problem_add_constraints handle constraint_system

Updates the PIP Problem referenced by `handle` so that the feasible region is represented by the original constraint system together with all the constraints in `constraint_system`.

ppl_PIP_Problem_set_big_parameter_dimension handle dimension

Sets the dimension for the big parameter to `dimension`.

ppl_PIP_Problem_get_big_parameter_dimension handle

Returns the dimension for the big parameter. Exception is thrown if no big parameter dimension has been set.

ppl_PIP_Problem_has_big_parameter_dimension handle

Returns true if and only if the dimension for the big parameter has been set.

ppl_PIP_Problem_is_satisfiable handle

Returns true if the PIP Problem referenced by `handle` is satisfiable and false otherwise.

ppl_PIP_Problem_solve handle

Solves the PIP problem referenced by `handle` and returns a status flag indicating the outcome of the optimization attempt: `Optimized_Pip_Problem` if the optimization attempt succeeds; `Unfeasible_Pip_Problem` otherwise.

ppl_PIP_Problem_solution handle

Solves the PIP problem referenced by `handle` and returns a handle to a PIP_Tree representing a feasible solution, if it exists and bottom otherwise.

ppl_PIP_Problem_optimizing_solution handle

Solves the PIP problem referenced by `handle` and returns a handle to a PIP_Tree representing an optimizing_solution, if it exists and bottom otherwise.

ppl_PIP_Problem_OK handle

Returns true if the PIP Problem referenced by `handle` is well formed, i.e., if it satisfies all its implementation invariants and false, otherwise. Useful for debugging purposes.

ppl_PIP_Problem_ascii_dump handle

Returns a string containing an ASCII dump of the internal representation of the PIP_Problem referenced by `handle`. Useful for debugging purposes.

ppl_PIP_Tree_Node_swap handle_1 handle_2

Swaps the PIP tree node referenced by `handle_1` with the one referenced by `handle_2`.

ppl_PIP_Tree_Node_OK handle

Returns true if the PIP tree node referenced by `handle` is well formed, i.e., if it satisfies all its implementation invariants and false, otherwise. Useful for debugging purposes.

ppl_PIP_Tree_Node_ascii_dump handle

Returns a string containing an ASCII dump of the internal representation of the Pip tree node referenced by `handle`. Useful for debugging purposes.

ppl_PIP_Tree_Node_constraints handle

Returns a list of the parameter constraints in the PIP tree node referenced by `handle`.

ppl_PIP_Tree_Node_artificials handle

Returns a list of the artificial parameters in the PIP tree node referenced by `handle`.

ppl_PIP_Tree_Node_is_bottom handle

Returns true if and only if `handle` represents bottom.

ppl_PIP_Tree_Node_is_decision handle

Returns true if and only if `handle` represents a decision node.

ppl_PIP_Tree_Node_is_solution handle

Returns true if and only if `handle` represents a solution node.

ppl_PIP_Tree_Node_parametric_values handle var

Returns a linear expression representing the values of problem variable `var` in the solution node represented by `handle`. The returned linear expression may involve problem parameters as well as artificial parameters.

ppl_PIP_Tree_Node_true_child handle var

Returns a handle to the child on the true branch of the PIP tree node represented by `handle`.

ppl_PIP_Tree_Node_false_child handle var

Returns a handle to the child on the false branch of the PIP tree node represented by `handle`.

C_Polyhedron Functions

Here we describe the main functions available for PPL objects defining convex and closed polyhedra.

ppl_new_C_Polyhedron_from_space_dimension space_dimension universe_or_empty

Returns a handle to a C polyhedron $\mathcal{P}$ with `space_dimension` dimensions; it is empty or the universe polyhedron depending on whether `universe_or_empty` is `empty` or `universe`, respectively.

ppl_new_C_Polyhedron_from_C_Polyhedron handle

If `handle` refers to a C polyhedron $\mathcal{P}_1$, then the expression will returns a handle to a copy $\mathcal{P}_2$ of $\mathcal{P}_1$.

ppl_new_C_Polyhedron_from_NNC_Polyhedron handle

If `handle` refers to an NNC polyhedron $\mathcal{P}_1$, then the expression returns a handle to a copy $\mathcal{P}_2$ of $\mathcal{P}_1$.

When using `ppl_new_C_Polyhedron_from_NNC_Polyhedron/2`, care must be taken that the source polyhedron referenced by `handle` is topologically closed.

ppl_new_C_Polyhedron_from_constraints constraint_system

Returns a handle to a C polyhedron $\mathcal{P}$ represented by `constraint_system`.

ppl_new_C_Polyhedron_from_generators generator_system

Returns a handle to a C polyhedron $\mathcal{P}$ represented by `generator_system`.

ppl_Polyhedron_swap handle_1 handle_2

Swaps the polyhedron $\mathcal{P}$ referenced by `handle_1` with the polyhedron $\mathcal{Q}$ referenced by `handle_2`. The polyhedra $\mathcal{P}$ and $\mathcal{Q}$ must have the same topology.

ppl_Polyhedron_space_dimension handle

Returns the dimension of the vector space in which the polyhedron referenced by `handle` is embedded.

ppl_Polyhedron_affine_dimension handle

Returns the actual dimension of the polyhedron referenced by `handle`.

ppl_Polyhedron_get_constraints handle

Return a list of the constraints in the constraints system representing the polyhedron referenced by `handle`.

ppl_Polyhedron_get_minimized_constraints handle

Returns a minimized list of the constraints in the constraints system representing the polyhedron referenced by `handle`.

ppl_Polyhedron_get_generators handle

Returns a list of the generators in the generators system representing the polyhedron referenced by `handle`.

ppl_Polyhedron_get_minimized_generators handle

Returns a minimized list of the generators in the generators system representing the polyhedron referenced by `handle`.

ppl_Polyhedron_relation_with_constraint handle constraint

Returns the list of relations the polyhedron referenced by `handle` has with `constraint`. The possible relations and their meaning is given in Section *Relation-With Operators* of the main PPL user manual.

ppl_Polyhedron_relation_with_generator handle generator

Returns the list of relations the polyhedron referenced by `handle` has with `generator`. The possible relations and their meaning is given in Section *Relation-With Operators* of the main PPL user manual.

ppl_Polyhedron_is_empty handle

Returns true if the polyhedron referenced by `handle` is empty and false, otherwise.

ppl_Polyhedron_is_universe handle

Returns true if the polyhedron referenced by `handle` is the universe and false, otherwise.

ppl_Polyhedron_is_bounded handle

Returns true if the polyhedron referenced by `handle` is bounded and false, otherwise.

ppl_Polyhedron_contains_integer_point handle

Returns true if the polyhedron referenced by `handle` contains at least one integer point and false, otherwise.

ppl_Polyhedron_bounds_from_above handle lin_expr

Returns true if the polyhedron referenced by `handle` is bounded from above by `lin_expr` and false, otherwise.

ppl_Polyhedron_bounds_from_below handle lin_expr

Returns true if the polyhedron referenced by `handle` is bounded from below by `lin_expr` and false, otherwise.

ppl_Polyhedron_maximize handle lin_expr

Returns a record `bool_1 * coefficient_1 * coefficient_2 * bool_2` where: `bool_1` is true if the polyhedron P referenced by `handle` is not empty and `lin_expr` is bounded from above in P and false, otherwise. `coefficient_1` is the numerator of the supremum value and `coefficient_2` the denominator of the supremum value. If the supremum is also the maximum, `bool_2` is true and false, otherwise.

ppl_Polyhedron_maximize_with_point handle lin_expr

Returns a record `bool_1 * coefficient_1 * coefficient_2 * bool_2 * Point` `bool_1` is true if the polyhedron P referenced by `handle` is not empty and `lin_expr` is bounded from above in P and false, otherwise. `coefficient_1` is the numerator of the supremum value and `coefficient_2` the denominator of the supremum value. If the supremum is also the maximum, `bool_2` is true and false, otherwise. `Point` is the point or closure point where `lin_expr` reaches the supremum.

ppl_Polyhedron_minimize handle lin_expr

Returns a record `bool_1 * coefficient_1 * coefficient_2 * bool_2` `bool_1` is true if the polyhedron P referenced by `handle` is not empty and `lin_expr` is bounded from below in P and false, otherwise. `coefficient_1` is the numerator of the infinum value and `coefficient_2` the denominator of the infinum value. If the infinum is also the minimum, `bool_2` is true and false, otherwise.

ppl_Polyhedron_minimize_with_point handle lin_expr

Returns a record `bool_1 * coefficient_1 * coefficient_2 * bool_2` `bool_1` is true if the polyhedron P referenced by `handle` is not empty and `lin_expr` is bounded from below in P and false, otherwise. `coefficient_1` is the numerator of the infinum value and `coefficient_2` the denominator of the infinum value. If the infinum is also the minimum, `bool_2` is true and false, otherwise. `Point` is the point or closure point where `lin_expr` reaches the infinum.

ppl_Polyhedron_is_topologically_closed handle

Returns true if the polyhedron referenced by `handle` is topologically closed and false, otherwise.

ppl_Polyhedron_contains_Polyhedron handle_1 handle_2

Returns true if the polyhedron referenced by `handle_2` is included in or equal to the polyhedron referenced by `handle_1` and false, otherwise.

ppl_Polyhedron_strictly_contains_Polyhedron handle_1 handle_2

Returns true if the polyhedron referenced by `handle_2` is included in but not equal to the polyhedron referenced by `handle_1` and false, otherwise.

ppl_Polyhedron_is_disjoint_from_Polyhedron handle_1 handle_2

Returns true if the polyhedron referenced by `handle_1` is disjoint from the polyhedron referenced by `handle_2` and false, otherwise.

ppl_Polyhedron_equals_Polyhedron handle_1 handle_2

Returns true if the polyhedron referenced by `handle_1` is equal to the polyhedron referenced by `handle_2` and false, otherwise.

ppl_Polyhedron_OK handle

Returns true if the polyhedron referenced by `handle` is well formed, i.e., if it satisfies all its implementation invariants and false, otherwise. Useful for debugging purposes.

ppl_Polyhedron_add_constraint handle constraint

Updates the polyhedron referenced by `handle` to one obtained by adding `constraint` to its constraint system.

ppl_Polyhedron_add_generator handle generator

Updates the polyhedron referenced by `handle` to one obtained by adding `generator` to its generator system.

ppl_Polyhedron_add_constraints handle constraint_system

Updates the polyhedron referenced by `handle` to one obtained by adding to its constraint system the constraints in `constraint_system`.

ppl_C_Polyhedron_add_generators handle generator_system

Updates the polyhedron referenced by `handle` to one obtained by adding to its generator system the generators in `generator_system`.

ppl_Polyhedron_intersection_assign handle_1 handle_2

Assigns to the polyhedron referenced by `handle_1` its intersection with the polyhedron referenced by `handle_2`.

ppl_Polyhedron_poly_hull_assign handle_1 handle_2

Assigns to the polyhedron referenced by `handle_1` its poly-hull with the polyhedron referenced by `handle_2`.

ppl_Polyhedron_poly_difference_assign handle_1 handle_2

Assigns to the polyhedron referenced by `handle_1` its poly-difference with the polyhedron referenced by `handle_2`.

ppl_Polyhedron_affine_image handle var lin_expr coefficient

Transforms the polyhedron referenced by `handle` assigning the affine expression `lin_expr/coefficient` to `var`.

ppl_Polyhedron_affine_preimage handle var lin_expr coefficient

This is the inverse transformation to that for `ppl_affine_image`.

ppl_Polyhedron_bounded_affine_image handle var lin_expr_1 lin_expr_2 coefficient

Transforms the polyhedron referenced by `handle` assigning the image with respect to the transfer relation `lin_expr_1/coefficient <= var <= lin_expr_2/coefficient`.

ppl_Polyhedron_generalized_affine_image handle var Relation_Symbol lin_expr coefficient

Transforms the polyhedron referenced by `handle` assigning the generalized affine image with respect to the transfer function `var Relation_Symbol lin_expr/coefficient`.

ppl_Polyhedron_generalized_affine_image_lhs_rhs handle lin_expr_1 Relation_Symbol lin_expr_2

Transforms the polyhedron referenced by `handle` assigning the generalized affine image with respect to the transfer function `lin_expr_1 Relation_Symbol lin_expr_2`.

ppl_Polyhedron_time_elapse_assign handle_1 handle_2

Assigns to the polyhedron $\mathcal{P}$ referenced by `handle_1` the time-elapse $(\mathcal{P} \nearrow \mathcal{Q})$ with the polyhedron $\mathcal{Q}$ referenced by `handle_2`.

ppl_Polyhedron_BHRZ03_widening_assign handle_1 handle_2

If the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`, then `handle_1` will refer to the BHRZ03-widening of $\mathcal{P}_1$ with $\mathcal{P}_2$.

ppl_Polyhedron_BHRZ03_widening_assign_with_tokens handle_1 handle_2 c_unsigned_1

It is assumed that the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`; let $\mathcal{P}$ denote the BHRZ03-widening of $\mathcal{P}_1$ with $\mathcal{P}_2$, Assuming that the quantity t_1 given by `c_unsigned_1` is the number of tokens available, Then this function will return the number of tokens remaining at the end of the operation.

ppl_Polyhedron_limited_BHRZ03_extrapolation_assign handle_1 handle_2 constraint_system

If the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`, then `handle_1` will refer to the BHRZ03-extrapolation of $\mathcal{P}_1$ with $\mathcal{P}_2$ improved by enforcing the constraints in `constraint_system`.

ppl_Polyhedron_limited_BHRZ03_extrapolation_assign_with_tokens handle_1 handle_2 constraint_system c_unsigned_1

It is assumed that the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`; let $\mathcal{P}$ denote the BHRZ03-extrapolation of $\mathcal{P}_1$ with $\mathcal{P}_2$, improved by enforcing those constraints in `constraint_system`.

Assuming that the quantity t_1 given by `c_unsigned_1` is the number of tokens available, then this function will return the number of tokens t_2 remaining at the end of the operation.

ppl_Polyhedron_bounded_BHRZ03_extrapolation_assign handle_1 handle_2 constraint_system

If the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`, then `handle_1` will refer to the BHRZ03-extrapolation of $\mathcal{P}_1$ with $\mathcal{P}_2$ improved by enforcing the constraints in `constraint_system` together with all constraints of the form $\pm x \leq r$ and $\pm x < r$ that are satisfied by every point in $\mathcal{P}_1$.

ppl_Polyhedron_bounded_BHRZ03_extrapolation_assign_with_tokens handle_1 handle_2 constraint_system c_unsigned_1

It is assumed that the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`; let $\mathcal{P}$ denote the BHRZ03-extrapolation of $\mathcal{P}_1$ with $\mathcal{P}_2$ improved by enforcing those constraints in `constraint_system` together with all constraints of the form $\pm x \leq r$ and $\pm x < r$ that are satisfied by every point in $\mathcal{P}_1$.

Assuming that the quantity t_1 given by `c_unsigned_1` is the number of tokens available, this function will return the number of tokens t_2 remaining at the end of the operation.

ppl_Polyhedron_H79_widening_assign handle_1 handle_2

If the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`, then `handle_1` will refer to the H79-widening of $\mathcal{P}_1$ with $\mathcal{P}_2$.

ppl_Polyhedron_H79_widening_assign_with_tokens handle_1 handle_2 c_unsigned_1

It is assumed that the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`; let $\mathcal{P}$ denote the H79-widening of $\mathcal{P}_1$ with $\mathcal{P}_2$, Assuming that the quantity t_1 given by `c_unsigned_1` is the number of tokens available, Then this function will return the number of tokens remaining at the end of the operation.

ppl_Polyhedron_limited_H79_extrapolation_assign handle_1 handle_2 constraint_system

If the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`, then `handle_1` will refer to the H79-extrapolation of $\mathcal{P}_1$ with $\mathcal{P}_2$ improved by enforcing the constraints in `constraint_system`.

ppl_Polyhedron_limited_H79_extrapolation_assign_with_tokens handle_1 handle_2 constraint_system c_unsigned_1

It is assumed that the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`; let $\mathcal{P}$ denote the H79-extrapolation of $\mathcal{P}_1$ with $\mathcal{P}_2$, improved by enforcing those constraints in `constraint_system`.

Assuming that the quantity t_1 given by `c_unsigned_1` is the number of tokens available, then this function will return the number of tokens t_2 remaining at the end of the operation.

ppl_Polyhedron_bounded_H79_extrapolation_assign handle_1 handle_2 constraint_system

If the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`, then `handle_1` will refer to the H79-extrapolation of $\mathcal{P}_1$ with $\mathcal{P}_2$ improved by enforcing the constraints in `constraint_system` together with all constraints of the form $\pm x \leq r$ and $\pm x < r$ that are satisfied by every point in $\mathcal{P}_1$.

ppl_Polyhedron_bounded_H79_extrapolation_assign_with_tokens handle_1 handle_2 constraint_system c_unsigned_1

It is assumed that the polyhedron $\mathcal{P}_1$ referenced by `handle_1` contains the polyhedron $\mathcal{P}_2$ referenced by `handle_2`; let $\mathcal{P}$ denote the H79-extrapolation of $\mathcal{P}_1$ with $\mathcal{P}_2$, improved by enforcing those constraints in `constraint_system` together with all constraints of the form $\pm x \leq r$ and $\pm x < r$ that are satisfied by every point in $\mathcal{P}_1$.

Assuming that the quantity t_1 given by `c_unsigned_1` is the number of tokens available, this function will return the number of tokens t_2 remaining at the end of the operation.

ppl_Polyhedron_topological_closure_assign handle

Assigns to the polyhedron referenced by `handle` its topological closure.

ppl_Polyhedron_add_space_dimensions_and_embed handle space_dimension

Embeds the polyhedron referenced by `handle` in a space that is enlarged by `space_dimension` dimensions,

ppl_Polyhedron_concatenate_assign handle_1 handle_2

Updates the polyhedron $\mathcal{P}_1$ referenced by `handle_1` by first embedding $\mathcal{P}_1$ in a new space enlarged by the space dimensions of the polyhedron $\mathcal{P}_2$ referenced by `handle_2`, and then adds to its system of constraints a renamed-apart version of the constraints of $\mathcal{P}_2$.

ppl_Polyhedron_add_space_dimensions_and_project handle space_dimension

Projects the polyhedron referenced by `handle` onto a space that is enlarged by `space_dimension` dimensions,

ppl_Polyhedron_remove_space_dimensions handle Int_List

Removes the space dimensions given by the identifiers of the PPL variables in list `Int_List` from the polyhedron referenced by `handle`. The identifiers for the remaining PPL variables are renumbered so that they are consecutive and the maximum index is less than the number of dimensions.

ppl_Polyhedron_remove_higher_space_dimensions handle space_dimension

Projects the polyhedron referenced to by `handle` onto the first `space_dimension` dimensions.

ppl_Polyhedron_expand_space_dimension handle var space_dimension

space_dimension copies of the space dimension referenced by variable var are added to the polyhedron referenced to by handle.

ppl_Polyhedron_fold_space_dimensions handle list_of_vars var

The space dimensions referenced by the PPL variables in list list_of_vars are folded into the dimension referenced by var and removed. The result is undefined if list_of_vars does not have the properties described in Section *Folding Multiple Dimensions of the Vector Space into One Dimension* of the main PPL user manual.

ppl_Polyhedron_map_space_dimensions handle p_func

Maps the space dimensions of the polyhedron referenced by handle using the partial function defined by a list of pairs of integers p_func. The result is undefined if p_func does not encode a partial function with the properties described in Section *Mapping the Dimensions of the Vector Space* of the main PPL user manual.

ppl_Polyhedron_wrap_assign handle list_of_vars width representation overflow constraint_system complexity_threshold wrap_indicator

Transforms the polyhedron referenced by handle by wrapping the dimensions given by list_of_vars while respecting the specified width, representation and overflow behavior of all these variables. The parameter constraint_system represents the conditional or looping construct guard with respect to which wrapping is performed. The non-negative integer complexity_threshold and Boolean wrap_indicator allow control of the complexity/precision ratio; higher values for complexity_threshold will lead to possibly greater precision while a true value for wrap_indicator indicates that the space dimensions should be wrapped individually. See Section *Wrapping Operator* for a more detailed description of this operator.

ppl_Polyhedron_ascii_dump handle

Returns a string containing an ASCII dump of the internal representation of the polyhedron referenced by handle. Useful for debugging purposes.

OCamldoc Documentation

NOTE: the complete documentation for module Ppl_ocaml, including all the types and functions that were enabled at configuration time, is only available in the *configuration dependent* OCamldoc documentation. The configuration independent OCamldoc documentation only contains those types and functions that are always enabled, which are grouped into module Ppl_ocaml_globals. Also note that module Ppl_ocaml automatically includes module Ppl_ocaml_globals.

2 Module Ppl_ocaml_globals

```
exception PPL_arithmetic_overflow of string
```

```
exception PPL_timeout_exception
exception PPL_internal_error of string
exception PPL_unknown_standard_exception of string
exception PPL_unexpected_error of string
type degenerate_element =
  | Universe
  | Empty
type linear_expression =
  | Variable of int
  | Coefficient of Gmp.Z.t
  | Unary_Plus of linear_expression
  | Unary_Minus of linear_expression
  | Plus of linear_expression * linear_expression
  | Minus of linear_expression * linear_expression
  | Times of Gmp.Z.t * linear_expression
type linear_constraint =
  | Less_Than of linear_expression * linear_expression
  | Less_Or_Equal of linear_expression * linear_expression
  | Equal of linear_expression * linear_expression
  | Greater_Than of linear_expression * linear_expression
  | Greater_Or_Equal of linear_expression * linear_expression
type linear_generator =
  | Line of linear_expression
  | Ray of linear_expression
  | Point of linear_expression * Gmp.Z.t
  | Closure_Point of linear_expression * Gmp.Z.t
type linear_grid_generator =
  | Grid_Line of linear_expression
  | Grid_Parameter of linear_expression * Gmp.Z.t
  | Grid_Point of linear_expression * Gmp.Z.t
type poly_gen_relation =
  | Subsumes
type poly_con_relation =
  | Is_Disjoint
  | Strictly_Intersects
  | Is_Included
  | Saturates
type relation_with_congruence =
  | Is_Disjoint
  | Strictly_Intersects
  | Is_Included
type linear_congruence = linear_expression * linear_expression *
  Gmp.Z.t
type constraint_system = linear_constraint list
type generator_system = linear_generator list
type grid_generator_system = linear_grid_generator list
type congruence_system = linear_congruence list
type relation_symbol =
  | Less_Than_RS
  | Less_Or_Equal_RS
```

```
  | Equal_RS
  | Greater_Than_RS
  | Greater_Or_Equal_RS
type bounded_integer_type_overflow =
  | Overflow_Wraps
  | Overflow_Undefined
  | Overflow_Impossible
type bounded_integer_type_representation =
  | Unsigned
  | Signed_2_Complement
type bounded_integer_type_width =
  | Bits_8
  | Bits_16
  | Bits_32
  | Bits_64
  | Bits_128
type complexity_class =
  | Polynomial_Complexity
  | Simplex_Complexity
  | Any_Complexity
type optimization_mode =
  | Minimization
  | Maximization
type mip_problem_status =
  | Unfeasible_Mip_Problem
  | Unbounded_Mip_Problem
  | Optimized_Mip_Problem
type control_parameter_name =
  | Pricing
type control_parameter_value =
  | Pricing_Steepest_Edge_Float
  | Pricing_Steepest_Edge_Exact
  | Pricing_Textbook
type pip_problem_status =
  | Unfeasible_Pip_Problem
  | Optimized_Pip_Problem
type pip_problem_control_parameter_name =
  | Cutting_Strategy
  | Pivot_Row_Strategy
type pip_problem_control_parameter_value =
  | Cutting_Strategy_First
  | Cutting_Strategy_Deepest
  | Cutting_Strategy_All
  | Pivot_Row_Strategy_First
  | Pivot_Row_Strategy_Max_Column
val ppl_version_major : unit -> int
val ppl_version_minor : unit -> int
val ppl_version_revision : unit -> int
val ppl_version_beta : unit -> int
val ppl_version : unit -> string
```

```
val ppl_banner : unit -> string
val ppl_io_wrap_string : string -> int -> int -> int -> string
val ppl_max_space_dimension : unit -> int
val ppl_Coefficient_bits : unit -> int
val ppl_Coefficient_is_bounded : unit -> bool
val ppl_Coefficient_max : unit -> Gmp.Z.t
val ppl_Coefficient_min : unit -> Gmp.Z.t
val ppl_Linear_Expression_is_zero : linear_expression -> bool
val ppl_Linear_Expression_all_homogeneous_terms_are_zero :
  linear_expression -> bool
val ppl_set_rounding_for_PPL : unit -> unit
val ppl_restore_pre_PPL_rounding : unit -> unit
val ppl_irrational_precision : unit -> int
val ppl_set_irrational_precision : int -> unit
val ppl_set_timeout : int -> unit
val ppl_reset_timeout : unit -> unit
val ppl_set_deterministic_timeout : int -> unit
val ppl_reset_deterministic_timeout : unit -> unit
type mip_problem
val ppl_new_MIP_Problem_from_space_dimension : int -> mip_problem
val ppl_new_MIP_Problem :
  int ->
  constraint_system ->
  linear_expression ->
  optimization_mode -> mip_problem
val ppl_MIP_Problem_space_dimension : mip_problem -> int
val ppl_MIP_Problem_integer_space_dimensions : mip_problem -> int list
val ppl_MIP_Problem_constraints : mip_problem -> constraint_system
val ppl_MIP_Problem_add_space_dimensions_and_embed :
  mip_problem -> int -> unit
val ppl_MIP_Problem_add_to_integer_space_dimensions :
  mip_problem -> int list -> unit
val ppl_MIP_Problem_add_constraint : mip_problem -> linear_constraint -> unit
val ppl_MIP_Problem_add_constraints :
  mip_problem -> constraint_system -> unit
val ppl_MIP_Problem_set_objective_function :
  mip_problem -> linear_expression -> unit
val ppl_MIP_Problem_is_satisfiable : mip_problem -> bool
val ppl_MIP_Problem_solve : mip_problem -> mip_problem_status
val ppl_MIP_Problem_optimization_mode : mip_problem -> optimization_mode
val ppl_MIP_Problem_feasible_point : mip_problem -> linear_generator
val ppl_MIP_Problem_optimizing_point : mip_problem -> linear_generator
val ppl_MIP_Problem_objective_function : mip_problem -> linear_expression
val ppl_MIP_Problem_optimal_value : mip_problem -> Gmp.Z.t * Gmp.Z.t
val ppl_MIP_Problem_evaluate_objective_function :
```

```
  mip_problem ->
  linear_generator -> Gmp.Z.t * Gmp.Z.t
val ppl_MIP_Problem_OK : mip_problem -> bool
val ppl_MIP_Problem_clear : mip_problem -> unit
val ppl_MIP_Problem_set_optimization_mode :
  mip_problem -> optimization_mode -> unit
val ppl_MIP_Problem_set_control_parameter :
  mip_problem ->
  control_parameter_value -> unit
val ppl_MIP_Problem_get_control_parameter :
  mip_problem ->
  control_parameter_name ->
  control_parameter_value
val ppl_MIP_Problem_swap : mip_problem -> mip_problem -> unit
val ppl_MIP_Problem_ascii_dump : mip_problem -> string
type pip_problem
type pip_tree_node
type artificial_parameter = linear_expression * Gmp.Z.t
val ppl_new_PIP_Problem_from_space_dimension : int -> pip_problem
val ppl_new_PIP_Problem :
  int ->
  constraint_system ->
  int list -> pip_problem
val ppl_PIP_Problem_space_dimension : pip_problem -> int
val ppl_PIP_Problem_parameter_space_dimensions : pip_problem -> int list
val ppl_PIP_Problem_constraints : pip_problem -> constraint_system
val ppl_PIP_Problem_add_space_dimensions_and_embed :
  pip_problem -> int -> int -> unit
val ppl_PIP_Problem_add_to_parameter_space_dimensions :
  pip_problem -> int list -> unit
val ppl_PIP_Problem_add_constraint : pip_problem -> linear_constraint -> unit
val ppl_PIP_Problem_add_constraints :
  pip_problem -> constraint_system -> unit
val ppl_PIP_Problem_is_satisfiable : pip_problem -> bool
val ppl_PIP_Problem_solve : pip_problem -> pip_problem_status
val ppl_PIP_Problem_solution : pip_problem -> pip_tree_node
val ppl_PIP_Problem_optimizing_solution : pip_problem -> pip_tree_node
val ppl_PIP_Problem_get_big_parameter_dimension : pip_problem -> int
val ppl_PIP_Problem_set_big_parameter_dimension : pip_problem -> int -> unit
val ppl_PIP_Problem_has_big_parameter_dimension : pip_problem -> bool
val ppl_PIP_Problem_OK : pip_problem -> bool
val ppl_PIP_Problem_clear : pip_problem -> unit
val ppl_PIP_Problem_set_control_parameter :
  pip_problem ->
  pip_problem_control_parameter_value -> unit
val ppl_PIP_Problem_get_control_parameter :
  pip_problem ->
```

```
  pip_problem_control_parameter_name ->
  pip_problem_control_parameter_value
val ppl_PIP_Problem_swap : pip_problem -> pip_problem -> unit
val ppl_PIP_Problem_ascii_dump : pip_problem -> string
val ppl_PIP_Tree_Node_constraints : pip_tree_node -> constraint_system
val ppl_PIP_Tree_Node_artificials :
  pip_tree_node ->
  artificial_parameter list
val ppl_PIP_Tree_Node_ascii_dump : pip_tree_node -> string
val ppl_PIP_Tree_Node_OK : pip_tree_node -> bool
val ppl_PIP_Tree_Node_is_bottom : pip_tree_node -> bool
val ppl_PIP_Tree_Node_is_solution : pip_tree_node -> bool
val ppl_PIP_Tree_Node_parametric_values :
  pip_tree_node -> int -> linear_expression
val ppl_PIP_Tree_Node_is_decision : pip_tree_node -> bool
val ppl_PIP_Tree_Node_true_child : pip_tree_node -> pip_tree_node
val ppl_PIP_Tree_Node_false_child : pip_tree_node -> pip_tree_node
```

Compilation and Installation

When the Parma Polyhedra Library is configured, it tests for the existence of the OCaml system. If OCaml is correctly installed in a standard location, things are arranged so that the OCaml interface is built and installed.

3 GNU General Public License

Version 3, 29 June 2007

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5 Module Index

5.1 Modules

Here is a list of all modules:

OCaml Language Interface 39

6 Module Documentation

6.1 OCaml Language Interface

The Parma Polyhedra Library comes equipped with an interface for the OCaml language.

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